

ws2022_exam

Student Group

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Exercise E1 Resistance of a Wire by Resistivity**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 is used for electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I needed to operate it for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{and } R = \\ 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E2 Resistance of a Wire by Resistivity**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A heating element made of solid nichrome wire with a cross-section of 1.80 mm^2 is used for electric power dissipation (= heat flow) of $P=40 \text{ W}$ is necessary.

Determine the current I needed to operate it for heating elements.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

∴ Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ \frac{1}{4} d^2 \cdot \pi \quad R &= \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{and } R = \\ 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

Exercise E3 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. A digital display shows a temperature coefficient of resistance of a thermistor. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

$$R = 10 \text{ k}\Omega \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

The power transfer resistor P is the product of the current and the voltage. Therefore, a solution is to increase the heat flow up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot (1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2)$$

Exercise E4 Temperature-dependent Resistance**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A digital display shows a temperature coefficient of resistance of a thermistor. The thermistor has a resistance of $10 \text{ k}\Omega$ at 25°C . Its temperature coefficients are: $\alpha = 0.01 \text{ K}^{-1}$ and $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$.

Result: The temperature inside the refrigeration system can reach down to -40°C .

Calculate the resistance of the thermistor at -40°C .

$$R = 10 \text{ k}\Omega \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2)$$

The power transfer resistor P is the product of the current and the voltage. Therefore, a solution is to increase the heat flow up the refrigeration system.

Therefore, with constant U and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad | \quad \Delta T = T_{\text{end}} - T_{\text{start}} \\ R = 10 \text{ k}\Omega \cdot (1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2)$$

Exercise E5 Pure Resistor Network Simplification

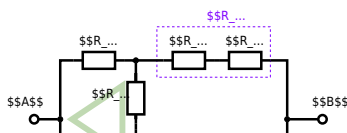
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall now be closed and integrated, $R_2 = R_3 = 100 \Omega$ and the switch between R_1 and R_2 shall be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution

$$R_{\text{eq}} = 133.8 \Omega$$

Now a wye-delta transformation is necessary.



Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:

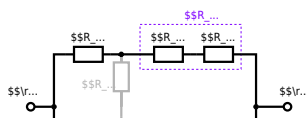
$$R_Y = \frac{R_2 \cdot R_3}{R_2 + R_3 + R_1} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) = 33.33 \Omega + (33.33 \Omega + 100 \Omega + 100 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_3) \parallel (R_2 + R_4) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega)$$

$$R_{eq} = \left\{ \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \right\} \parallel (100 \, \Omega + 100 \, \Omega) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (R_2 + R_4) \parallel (R_2 + R_1 + R_3)$$

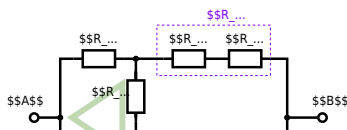
Exercise E6 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall be simplified with $R_1 = 200 \, \Omega$, $R_2 = 100 \, \Omega$, $R_3 = 150 \, \Omega$, $R_4 = 100 \, \Omega$ and the voltage source $U_{SV} = 10 \, \text{V}$.
Result given: $R_{eq} = 132.8 \, \Omega$.

Solution

$$R_{eq} = 132.8 \, \Omega$$

Now a wye-delta transformation is necessary.



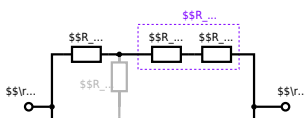
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$\begin{aligned} R_{\text{eq}} &= (R_2 + R_1 || R_3) || R_4 \\ R_{\text{eq}} &= (100 \, \Omega + 200 \, \Omega || 200 \, \Omega) || (100 \, \Omega + 100 \, \Omega) \\ R_{\text{eq}} &= (500 \, \Omega) || (200 \, \Omega) \\ R_{\text{eq}} &= \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega} \end{aligned}$$

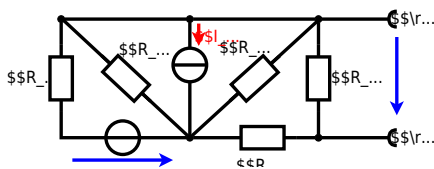
Exercise E7 Equivalent linear Source

(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.

Result

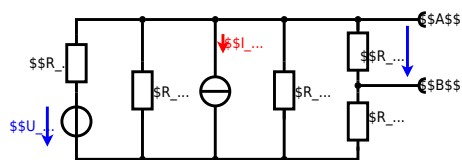
$$\begin{aligned} U_s &= U_{AB} = 4.5 \, \text{V} \\ R_i &= R_{AB} = 6 \, \Omega \end{aligned}$$



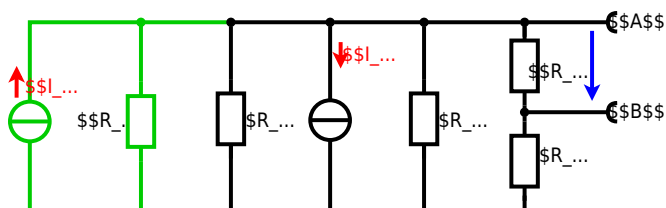
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $R_1=5.0 \, \Omega$, $U_2=6.0 \, \text{V}$, $R_3=10 \, \Omega$, $I_4=4.2 \, \text{A}$, $R_5=10 \, \Omega$, $R_6=7.5 \, \Omega$, $R_7=15 \, \Omega$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :
$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_{24}}{R_1} - I_4$$
 The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:
$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{24} = U_2 \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} - I_4 \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_6 , R_7 , and $R_1 \parallel R_3 \parallel R_5$.

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} - I_4 \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance (0Ω , so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5 \Omega \parallel 10 \Omega \parallel 10 \Omega = 5 \Omega \parallel 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \quad R_{AB} = 15 \Omega \parallel (7.5 \Omega + 2.5 \Omega)$$

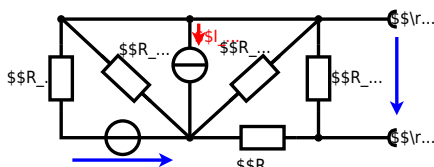
Exercise E8 Equivalent linear Source

(written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.

Result

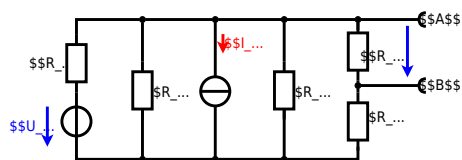
$$U_s = U_{AB} = 4.5 \text{ V} \quad R_i = R_{AB} = 6 \Omega$$



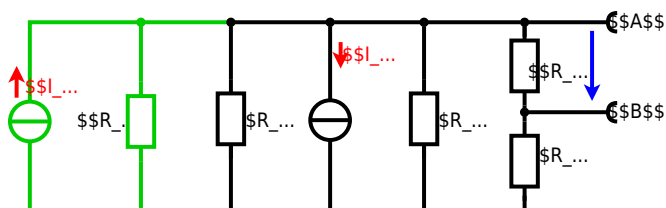
Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B. $R_1=5.0 \, \Omega$, $U_2=6.0 \, \text{V}$, $R_3=10 \, \Omega$, $I_4=4.2 \, \text{A}$, $R_5=10 \, \Omega$, $R_6=7.5 \, \Omega$, $R_7=15 \, \Omega$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$U_{AB} = R_{135} \cdot I_{24} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot R_1 \parallel R_3 \parallel R_5$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

Therefore the voltage between A and B is given as:

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = \left(\frac{U_2}{R_1} - I_4 \right) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance ($=0\Omega$, so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5\Omega \parallel 10\Omega \parallel 10\Omega = 5\Omega \parallel 5\Omega = 2.5\Omega$:

$$U_{AB} = \frac{6.0\text{V}}{5.0\Omega} - 4.2\Omega \cdot \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \quad R_{AB} = 15\Omega \parallel (7.5\Omega + 2.5\Omega)$$

Exercise E9 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit below is a battery with an internal resistance of $R_1 = 5\Omega$ and a charging capacitor $C = 2\mu\text{F}$ and a resistor $R_2 = 10\Omega$ in series. The voltage across the capacitor is again 0V at the moment $t_0 = 0\text{s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1\text{ms}$ after closing the switch.

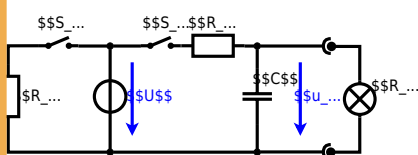
Result:

Hint: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

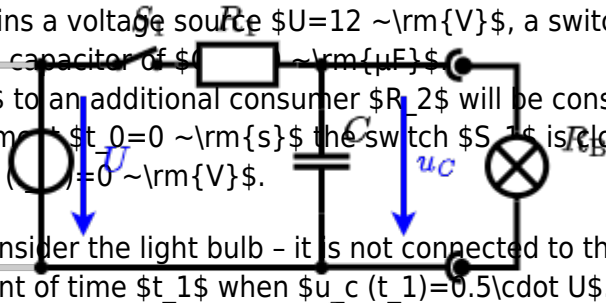
$$U_{\text{equiv}} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12\text{V} \cdot 10\Omega}{5\Omega + 10\Omega} = 8\text{V}$$

Solution: The circuit is a series circuit with a voltage source $U_{\text{equiv}} = 8\text{V}$ and a resistor $R_2 = 10\Omega$ in series. The voltage across the capacitor is again 0V at the moment $t_0 = 0\text{s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2 = 1\text{ms}$ after closing the switch.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .



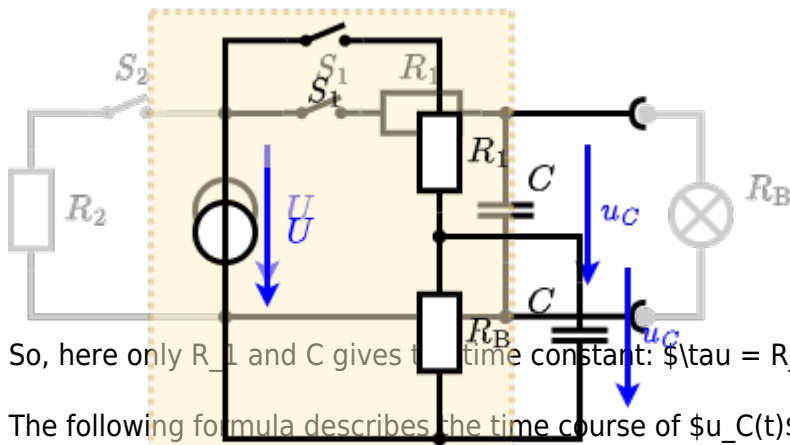
The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_c(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_c(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_c(t)$ which has to be $u_c(t_1)=0.5 \cdot U$:

$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$. An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

Exercise E10 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (see the solution) consists of a 12 V DC voltage source, a switch S_1 and a switch S_2 connected to a $20\text{ }\Omega$ resistor, a $100\text{ }\mu\text{F}$ capacitor and a $10\text{ }\Omega$ resistor. At the moment $t_0=0\text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_c(t_2)$ across the capacitor at $t_2=1\text{ ms}$ after closing the switch.

Solution

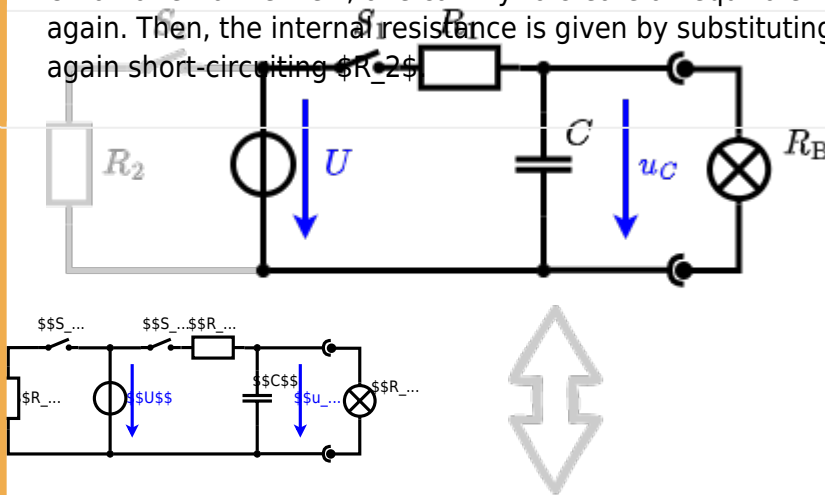
To solve this, first create an equivalent linear voltage source from U , R_1 , and R_B .

$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U = 6\text{ V}$$

Solution

The ideal voltage source is given by $U_s = U \cdot \frac{R_1}{R_1 + R_B}$ and the internal resistance is given by $R_i = R_1 \parallel R_B$.

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

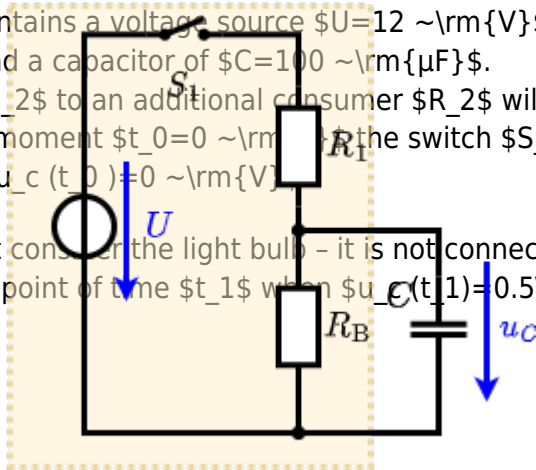


The circuit contains a voltage source $U = 12 \text{ V}$, a switch S_1 , a resistor of $R_1 = 20 \text{ }\Omega$ and a capacitor of $C = 100 \text{ }\mu\text{F}$.

The switch S_2 to an additional consumer R_2 will be considered to be open for the first tasks. At the moment $t_0 = 0$ the switch S_1 is closed, the voltage across the capacitor is $u_C(t_0) = 0 \text{ V}$.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time t_1 when $u_C(t_1) = 0.5 \cdot U$.



Solution

An equivalent linear voltage source can be given with U_s , R_1 , and R_B as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($R_i = 0 \text{ }\Omega$, short-circuit).

$$R_i = R_1 \parallel R_B = 10 \text{ }\Omega$$

$$u_C(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-t_2/(10 \text{ }\Omega \cdot 100 \text{ }\mu\text{F})})$$

So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_C(t_1) = 0.5 \cdot U$:

$$u_C(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$

It has to be rearranged to t :

$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(0.5)$$

Exercise E11 Analyzing complex Impedances

(written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (φ and $\underline{X}_L$) shall be given.

After analysis, the full bridge dimensioned circuit impedance can be extracted and the phase angle φ in phase (calculated) $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$ and $\underline{X}_L = 2\pi f L = 2\pi \cdot 300 \cdot 7.8 \cdot 10^{-3} = 14.68 \Omega$

.. Calculate the physical values of the two components.

Solution $\underline{R} = 0.24 \Omega$ and $\underline{X}_L = 14.68 \Omega$ and $\varphi = -10.9^\circ$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.4 \angle 10.9^\circ$ A

The current and voltage are in phase since the impedance is purely real (no imaginary part). The resulting impedance is $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 4.68Ω is a capacitor with the same absolute value of 4.68Ω but with a negative sign. The impedance is $\underline{Z} = 0.24 - j4.68 \Omega$.

The phase angle φ is calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$.

The physical values are $R = 0.24 \Omega$ and $X_L = 14.68 \Omega$.

With the complex part (complex value) $\underline{Z} = 0.24 - j4.68 \Omega$ and $\underline{U} = 50 \angle 0^\circ$ V, the phase angle φ can be calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$.

Exercise E12 Analyzing complex Impedances

(written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phase angle of the solution $\underline{U} = 50 \angle 0^\circ$ mV and $\underline{Z} = 0.24 - j4.68 \Omega$ in both the components. (φ and $\underline{X}_L$) shall be given.

After analysis, the full bridge dimensioned circuit impedance can be extracted and the phase angle φ in phase (calculated) $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$ and $\underline{X}_L = 2\pi f L = 2\pi \cdot 300 \cdot 7.8 \cdot 10^{-3} = 14.68 \Omega$

.. Calculate the physical values of the two components.

Solution $\underline{R} = 0.24 \Omega$ and $\underline{X}_L = 14.68 \Omega$ and $\varphi = -10.9^\circ$

Solution

$\underline{I} = \frac{\underline{U}}{\underline{Z}} = \frac{50 \angle 0^\circ}{0.24 - j4.68} = 10.4 \angle 10.9^\circ$ A

The current and voltage are in phase since the impedance is purely real (no imaginary part). The resulting impedance is $\underline{Z} = 0.24 - j4.68 \Omega$.

Therefore, the component 4.68Ω is a capacitor with the same absolute value of 4.68Ω but with a negative sign. The impedance is $\underline{Z} = 0.24 - j4.68 \Omega$.

The phase angle φ is calculated as $\varphi = \arctan\left(\frac{-4.68}{0.24}\right) = -10.9^\circ$.

The physical values are $R = 0.24 \Omega$ and $X_L = 14.68 \Omega$.

The absolute value of the impedance is $Z = \sqrt{(0.24 \sim \Omega)^2 + (4.68 \sim \Omega)^2} = 4.7 \sim \Omega$
 The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$
 With the complex part comes the physical value: $X_L = \omega L = 2\pi \cdot 4.7 \sim \Omega$
 The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$

Exercise E13 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

A series circuit means that the current is constant on every component.
 The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$
 Parallel circuit means that the voltage is the same on R_3 and C_2
 The equivalent impedance for R_3 and C_2 combined is given by $Z = \frac{R_3 \cdot X_C}{R_3 + X_C}$
 Back to the first formula: $R_3 \cdot Z = X_C \cdot Z$
 The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$

Solution

$R_1 = 1.00 \sim \Omega$

$R_2 = 10.0 \sim \Omega$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by $Z = \sqrt{R^2 + X_L^2}$

Parallel circuit means that the voltage is the same on R_3 and C_2
 The equivalent impedance for R_3 and C_2 combined is given by $Z = \frac{R_3 \cdot X_C}{R_3 + X_C}$
 Back to the first formula: $R_3 \cdot Z = X_C \cdot Z$

The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$

Therefore, the resulting current of the parallel circuit is given as:

$I = \frac{U}{Z} = \frac{10 \text{ V}}{\sqrt{1.00^2 + 10.0^2}} = 0.99 \text{ A}$

This current is the same on R_2 and C_2
 The voltage across R_2 is $U_R = I \cdot R_2 = 9.9 \text{ V}$

Back to the first formula: $R_3 \cdot Z = X_C \cdot Z$

The phase φ is $\varphi = \arctan\left(\frac{4.68}{0.24}\right) = 87.1^\circ$

Exercise E14 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Reactive power is the real resistor value of $20 \pm 3 \text{ m}\Omega$ in parallel with a capacitor having impedance of $35 \pm 3 \text{ }\Omega$. B.O
 $\sim \text{m}\Omega$, $\text{fitB} = 200 \pm 45 \text{ m}\Omega$, Hz high-gate test current $\text{fitB} = 50 \text{ }\mu\text{A}$ $\sim \text{m}\Omega$ through
 a resistor R_1 shall have the same absolute value of the impedance as a capacitor
 $C_1 = 40 \text{ nF}$ at $f_1 = 4 \text{ MHz}$.

$$R_1 \approx 1.00 \sim \Omega$$
$$\text{solution} \begin{array}{l} \text{begin}\{align*\\ R \geq 10.0 \\ \end{array}$$

Solution

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by \begin{align*}

Parallel circuit means that the voltage is the same on \$R_1\$ and \$R_2\$. $V = R_1 I_1 = R_2 I_2$ and $I = I_1 + I_2$.
 Series circuit means that the current is the same through \$R_1\$ and \$R_2\$. $I = I_1 = I_2$ and $V = V_1 + V_2$.
 The voltage divider rule states that the voltage across a resistor in a series circuit is proportional to its resistance.
 The current divider rule states that the current through a resistor in a parallel circuit is proportional to its conductance.
 The power in a resistor is given by $P = I^2 R = V^2 / R$.
 The maximum average power transfer theorem states that the maximum average power is transferred to a load when the load impedance is the complex conjugate of the source impedance.
 Thevenin's theorem states that any linear circuit with voltage and current sources and resistors can be replaced by an equivalent circuit consisting of a voltage source in series with a resistor.
 Norton's theorem states that any linear circuit with voltage and current sources and resistors can be replaced by an equivalent circuit consisting of a current source in parallel with a resistor.
 The superposition theorem states that the response in any element of a linear circuit with multiple independent sources is the sum of the responses caused by each independent source acting alone, with all other independent sources replaced by their internal impedances.
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 Thevenin's theorem states that any linear circuit with voltage and current sources and resistors can be replaced by an equivalent circuit consisting of a voltage source in series with a resistor.
 Norton's theorem states that any linear circuit with voltage and current sources and resistors can be replaced by an equivalent circuit consisting of a current source in parallel with a resistor.
 The superposition theorem states that the response in any element of a linear circuit with multiple independent sources is the sum of the responses caused by each independent source acting alone, with all other independent sources replaced by their internal impedances.

\$\{ \mathbf{v}_1, \mathbf{v}_2 \}\$ can be simplified to: $\text{begin}(\text{angle}, \text{vert})$
 $\{ \mathbf{v}_1, \mathbf{v}_2 \} \perp \{ \mathbf{u}_1, \mathbf{u}_2 \}$ (It has to, since $\mathbf{R}_3$
 is perpendicular to $\{ \mathbf{v}_1, \mathbf{v}_2 \}$ and $\{ \mathbf{u}_1, \mathbf{u}_2 \}$ too)
 $\text{end}(\text{angle}, \text{vert})$

Therefore, the resulting current of the parallel circuit is given as: \begin{align*}

$$\underline{I}^3 = \underline{I}^{3R} + \underline{I}^{3C} \quad \forall$$
[illegible]
$$\right)^2 - (2\pi \cdot 450 \sim \{\rm kHz\} \cdot 4.7 \sim \{\rm \mu H\})^2 \} \\\end{align*}$$

Back to the first formula:
$$R_3 \cdot I_{3R} = X_{3C} \cdot$$

$$\{I\} \setminus \{3C\} \cap R \subseteq \{X\} \setminus \{3C\} \cdot \frac{\{I\} \setminus \{3C\}}{\{I\} \setminus \{3R\}} \cap \{3C\} \cap R$$
$$\frac{1}{2\pi i} \oint_{\Gamma} \frac{f(z)}{z^3} dz \cdot \sqrt{|I|} \cdot |3| \cdot \frac{1}{2} =$$
$$\frac{| \{I\} \setminus \{3R\} |^2}{| \{I\} \setminus \{3R\} |} \quad \parallel \quad \text{\texttt{\textbackslash end\{align*\}}}$$

Exercise E15 Complex Impedance Circuit

(written test, approx. 15 % of a 60-minute written test, WS2022)

2. Calculate the three (full) periods for $\text{size}(\text{Z})$, $\text{bandwidth}(\text{Z})$ and

Problem 5.7) A cylindrical capacitor of length $l = 1.0 \text{ m}$ and radii $a = 1.0 \text{ cm}$ and $b = 2.0 \text{ cm}$ is connected to a 10 V battery. The space between the cylinders is filled with a dielectric material with a dielectric constant $\epsilon_r = 2.0$. Calculate the capacitance C and the electric field E in the dielectric.

Solution
This linear source is connected with an inductor of $330 \sim \{\rm \mu H\}$ and a capacitor of $0.22 \sim \{\rm \mu F\}$, all in series.

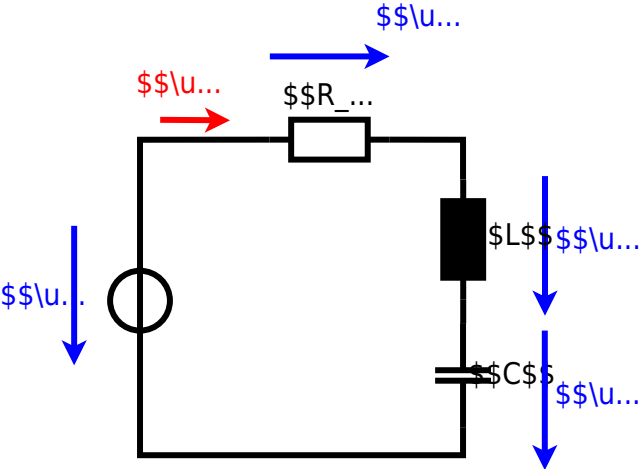
Result

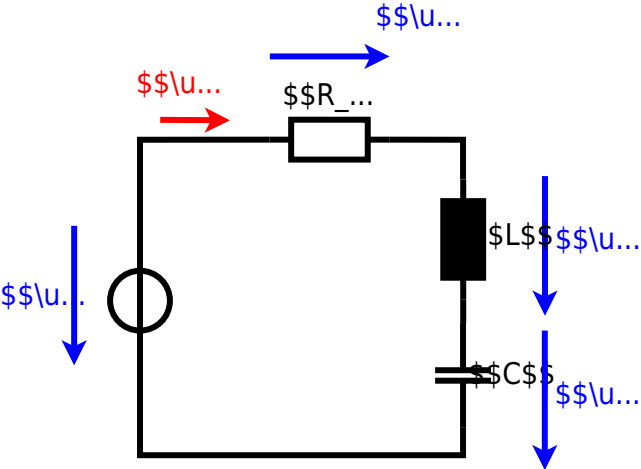
$$\begin{aligned} \begin{array}{l} \text{\tiny \rm \textit{begin{align*}}} \\ \text{\tiny \rm \textit{end{align*}}} \end{array} \quad Z = 19.7 \sim \Omega \quad \text{\tiny \rm \textit{begin{align*}}} \quad Z = 48.2 \sim \Omega \quad \text{\tiny \rm \textit{end{align*}}} \quad Z = 19.8 \sim \Omega \end{aligned}$$

label all components, voltages, and currents.

$$\begin{aligned} Z &= \{ \{ \hat{U} \} \over \{ \hat{I} \} \} \} \parallel \hat{I} = \{ \{ \hat{U} \} \over \{ Z \} \} \parallel \end{aligned}$$
$$\{Z \mid C \models \{ \{1\} \over 2\pi \cdot f \cdot C \} \} \models \{ \{1\} \over 2\pi \cdot 15 \}$$
$$\text{result} \{\rm kHz\} \cdot 0.22 \sim \{\rm \mu F\}$$
[illegible]
$$\frac{\{1\} \overline{\sqrt{2}}}{\{1\} \overline{\sqrt{2}}} \cdot \frac{\{\hat{U}\} \overline{Z}}{\{\hat{U}\} \overline{Z}} \cdot \frac{\{1\} \overline{\sqrt{2}}}{\{1\} \overline{\sqrt{2}}}$$
$$\forall \theta \in [0, \pi] \quad \frac{\|f(\theta)\|}{\|\Omega\|} \leq \frac{1}{2\pi} \int_0^{2\pi} \|f(t)\| dt$$
$$\sim \{\mathrm{rm\ kHz}\} \cdot 330 \sim \{\mathrm{rm\ \mu H}\} \} \} \end{align*}$$
$$\begin{aligned} \underline{Z} &= R + \underline{Z} \quad L + \underline{Z} \quad C \end{aligned}$$
[illegible]
$$\sqrt{R^2 + (\underline{Z}^L - \underline{Z}^C)^2}$$







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Last update: **2023/04/02 00:45**

