

# task\_7el8zljglaazxtw\_with\_calculation

## Student Group

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resonant circuit, exam ee2 SS2022

**Exercise E14 Series Resonant Circuit**  
**(written test, approx. 10 % of a 120-minute written test, SS2022)**

2. What is the resonance frequency of the series RLC circuit shown in the circuit diagram? The resistance of the resistor is  $R = 100 \text{ } \Omega$ , the inductance of the inductor is  $L = 60 \text{ } \mu\text{H}$ , and the capacitance of the capacitor is  $C = 10 \text{ nF}$ .

At resonance, the impedance of the series RLC circuit would be  $Z_{RLC} = R$ . Which value would  $f_0$  have for the given  $R$ ?

Path:  $C = 10 \text{ nF}$

$R = 100 \text{ } \Omega$

Path:  $L = 60 \text{ } \mu\text{H}$

The resonance frequency is given as  $f_0 = \frac{1}{2\pi\sqrt{LC}}$

With values:  $C = 10 \text{ nF} = 10 \cdot 10^{-9} \text{ F}$ ,  $L = 60 \text{ } \mu\text{H} = 60 \cdot 10^{-6} \text{ H}$

$f_0 = \frac{1}{2\pi\sqrt{60 \cdot 10^{-6} \cdot 10 \cdot 10^{-9}}}$

$f_0 = \frac{1}{2\pi\sqrt{600 \cdot 10^{-15}}}$

$f_0 = \frac{1}{2\pi\sqrt{6 \cdot 10^{-13}}}$

$f_0 = \frac{1}{2\pi \cdot \sqrt{6} \cdot 10^{-6.5}}$

$f_0 = \frac{1}{2\pi \cdot 2.45 \cdot 10^{-6.5}}$

$f_0 = \frac{1}{4.9 \cdot 10^{-6.5}}$

$f_0 = \frac{10^{6.5}}{4.9}$

$f_0 = \frac{3.16 \cdot 10^6}{4.9}$

$f_0 = 64.5 \text{ kHz}$

1. What is the impedance  $Z_{RLC}$  of this real capacitor for  $f_0 = 100 \text{ MHz}$ ? (Phase and magnitude)

Path

The impedance  $Z_{RLC}$  is given by:  $Z_{RLC} = R + j\omega L - \frac{j}{\omega C}$

Putting in the numbers, only for the reactive part  $X_{LC}$ :

$X_{LC} = 2\pi \cdot 100 \cdot 10^6 \cdot 10 \cdot 10^{-9} - \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot 60 \cdot 10^{-6}}$

$X_{LC} = 2\pi \cdot 100 \cdot 10^6 \cdot 10^{-8} - \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot 60 \cdot 10^{-6}}$

$X_{LC} = 2\pi \cdot 10^6 \cdot 10^{-2} - \frac{1}{2\pi \cdot 10^8 \cdot 60 \cdot 10^{-6}}$

$X_{LC} = 2\pi \cdot 10^4 - \frac{1}{2\pi \cdot 60 \cdot 10^2}$

$X_{LC} = 62831.85 - \frac{1}{376.99}$

$X_{LC} = 62831.85 - 0.00265$

$X_{LC} = 62831.85 \text{ } \Omega$

With the real and imaginary parts, we can derive the magnitude and phase:

$$\begin{aligned} Z_{\text{RLC}} &= \sqrt{R^2 + X_{\text{LC}}^2} \quad \parallel \quad = \sqrt{(88 \text{ m}\Omega)^2 + (-121.45 \text{ m}\Omega)^2} \quad \parallel \quad = 150.0... \text{ m}\Omega \\ \end{aligned}$$

$$\begin{aligned} \varphi &= \arctan \left( \frac{X_{\text{LC}}}{R} \right) \quad \parallel \quad = \arctan \left( \frac{-121.45 \text{ m}\Omega}{88 \text{ m}\Omega} \right) \quad \parallel \quad = -0.9437... \\ &= -54.07...^\circ \quad \parallel \quad \end{aligned}$$

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