

task_wjttvmydrskzhcim_with_calculation

Student Group

First Name	Surname	Matrikel Nr.

Table of Contents

Exercise E22 Component Parameters (written test, approx. 10 % of a 120-minute written test, SS2021) 2

complex voltage divider, RMS, inductor, exam ee2 SS2021

Exercise E22 Component Parameters**(written test, approx. 10 % of a 120-minute written test, SS2021)**

For the next exercises consider the following circuit. The motor presents a resistive inductance and a series resistance R_{M} and the inductance L_{M} are determined below. Both results in the impedance of the motor.

This resulted in the recorded current of

a) Derive in general the equation for the absolute value of the impedance of the motor.

$$|Z| = \sqrt{(2\pi \cdot f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

$$R_{\text{M}} = 4.3301 \cdot \Omega$$

$$L_{\text{M}} = 14.346 \cdot \text{mH}$$

b) Since we have $|Z_1|$ and $|Z_2|$ from b) we can subtract two of the formulas from a) and this has the advantage that R_{M} will cancel out:

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - \left((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 \right)$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

The complex impedance $\underline{Z}$ for a resistive inductive load is $\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$ and the series circuit is given as

$$\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$$

Now we can rearrange to L_{M} :

The Pythagorean theorem can derive the absolute value:

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

And then to L_{M} :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{|Z_2|^2 - |Z_1|^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10 \cdot \Omega)^2 - (6.25 \cdot \Omega)^2}{(100 \cdot \text{s}^{-1})^2 - (50 \cdot \text{s}^{-1})^2}} = 14.346 \cdot \text{mH}$$

The resistance value R_{M} can be derived from $|Z_2|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2$

$$R_{\text{M}} = \sqrt{(10 \cdot \Omega)^2 - (2\pi \cdot 100 \cdot \text{s}^{-1} \cdot 0.014346 \cdot \text{H})^2} = 4.3301 \cdot \Omega$$

From:
<https://first.mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:
https://first.mexle.te.hs-heilbronn.de/electrical_engineering_and_electronics/task_wjttvmydrskzhcim_with_calculation

Last update: **2024/07/04 01:51**

