

# Exam Winter Semester 2022

## Student Group

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# Exam Winter Semester 2022

## Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

## Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

## Only EEE1-relevant Part

**This part is only for about 25 minutes !**

### Exercise E1 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. Heating elements are used to heat wire with a temperature of  $180^\circ\text{C}$ . An electric power dissipation (= heat flow) of  $P=40\text{ W}$  is necessary.

Determine the current  $I$  needed to operate for heating elements.

The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6}\ \Omega\text{m}$ .

The heating element is  $3\text{ m}$  long and has a diameter of  $3.57\text{ mm}$ .

∴ Calculate the resistance  $R$  of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \\ &= \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{ W}}{0.33\ \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \text{with } A = r^2 \cdot \pi = \\ &= \frac{1}{4} d^2 \cdot \pi \quad \text{and } R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad \text{and } R = \\ &= 1.10 \cdot 10^{-6}\ \Omega\text{m} \cdot \frac{4 \cdot 3\text{ m}}{(3.57 \cdot 10^{-3}\text{ m})^2 \cdot \pi} \end{aligned}$$

**Exercise E2 Temperature-dependent Resistance**  
**(written test, approx. 6 % of a 60-minute written test, WS2022)**

2. A refrigerator, which has a temperature coefficient of resistance in the refrigeration system. The thermistor has a resistance of  $10 \text{ k}\Omega$  at  $25^\circ\text{C}$ . Its temperature coefficients are:  $\alpha = 0.01 \text{ K}^{-1}$  and  $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$ .

Result: The temperature inside the refrigeration system can reach down to  $-40^\circ\text{C}$ .

Result: Calculate the resistance of the thermistor at  $-40^\circ\text{C}$ .

Result:  $R = 6.5 \text{ k}\Omega$

Resistance transfer characteristic of the circuit and of the heat flow. Therefore, a solution is to increase the heat flow up the refrigeration system.

Therefore, with constant  $U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

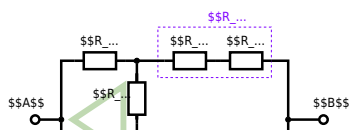
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\begin{align*} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) && | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} && \\ R &= 10 \text{ k}\Omega \cdot \left(1 + 0.01 \text{ K}^{-1} \cdot (-40^\circ\text{C} - 25^\circ\text{C}) + 71 \cdot 10^{-6} \text{ K}^{-2} \cdot (-40^\circ\text{C} - 25^\circ\text{C})^2\right) && \\ &&& \end{align*}
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**Exercise E4 Pure Resistor Network Simplification**  
**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following shall be solved at  $0^\circ\text{C}$ .  $R_1 = 10 \text{ }\Omega$ ,  $R_2 = 10 \text{ }\Omega$ ,  $R_3 = 10 \text{ }\Omega$ ,  $R_4 = 10 \text{ }\Omega$ ,  $R_5 = 10 \text{ }\Omega$ ,  $R_6 = 10 \text{ }\Omega$ ,  $R_7 = 10 \text{ }\Omega$ ,  $R_8 = 10 \text{ }\Omega$ ,  $R_9 = 10 \text{ }\Omega$ ,  $R_{10} = 10 \text{ }\Omega$ ,  $R_{11} = 10 \text{ }\Omega$ ,  $R_{12} = 10 \text{ }\Omega$ ,  $R_{13} = 10 \text{ }\Omega$ ,  $R_{14} = 10 \text{ }\Omega$ ,  $R_{15} = 10 \text{ }\Omega$ ,  $R_{16} = 10 \text{ }\Omega$ ,  $R_{17} = 10 \text{ }\Omega$ ,  $R_{18} = 10 \text{ }\Omega$ ,  $R_{19} = 10 \text{ }\Omega$ ,  $R_{20} = 10 \text{ }\Omega$ ,  $R_{21} = 10 \text{ }\Omega$ ,  $R_{22} = 10 \text{ }\Omega$ ,  $R_{23} = 10 \text{ }\Omega$ ,  $R_{24} = 10 \text{ }\Omega$ ,  $R_{25} = 10 \text{ }\Omega$ ,  $R_{26} = 10 \text{ }\Omega$ ,  $R_{27} = 10 \text{ }\Omega$ ,  $R_{28} = 10 \text{ }\Omega$ ,  $R_{29} = 10 \text{ }\Omega$ ,  $R_{30} = 10 \text{ }\Omega$ ,  $R_{31} = 10 \text{ }\Omega$ ,  $R_{32} = 10 \text{ }\Omega$ ,  $R_{33} = 10 \text{ }\Omega$ ,  $R_{34} = 10 \text{ }\Omega$ ,  $R_{35} = 10 \text{ }\Omega$ ,  $R_{36} = 10 \text{ }\Omega$ ,  $R_{37} = 10 \text{ }\Omega$ ,  $R_{38} = 10 \text{ }\Omega$ ,  $R_{39} = 10 \text{ }\Omega$ ,  $R_{40} = 10 \text{ }\Omega$ ,  $R_{41} = 10 \text{ }\Omega$ ,  $R_{42} = 10 \text{ }\Omega$ ,  $R_{43} = 10 \text{ }\Omega$ ,  $R_{44} = 10 \text{ }\Omega$ ,  $R_{45} = 10 \text{ }\Omega$ ,  $R_{46} = 10 \text{ }\Omega$ ,  $R_{47} = 10 \text{ }\Omega$ ,  $R_{48} = 10 \text{ }\Omega$ ,  $R_{49} = 10 \text{ }\Omega$ ,  $R_{50} = 10 \text{ }\Omega$ ,  $R_{51} = 10 \text{ }\Omega$ ,  $R_{52} = 10 \text{ }\Omega$ ,  $R_{53} = 10 \text{ }\Omega$ ,  $R_{54} = 10 \text{ }\Omega$ ,  $R_{55} = 10 \text{ }\Omega$ ,  $R_{56} = 10 \text{ }\Omega$ ,  $R_{57} = 10 \text{ }\Omega$ ,  $R_{58} = 10 \text{ }\Omega$ ,  $R_{59} = 10 \text{ }\Omega$ ,  $R_{60} = 10 \text{ }\Omega$ ,  $R_{61} = 10 \text{ }\Omega$ ,  $R_{62} = 10 \text{ }\Omega$ ,  $R_{63} = 10 \text{ }\Omega$ ,  $R_{64} = 10 \text{ }\Omega$ ,  $R_{65} = 10 \text{ }\Omega$ ,  $R_{66} = 10 \text{ }\Omega$ ,  $R_{67} = 10 \text{ }\Omega$ ,  $R_{68} = 10 \text{ }\Omega$ ,  $R_{69} = 10 \text{ }\Omega$ ,  $R_{70} = 10 \text{ }\Omega$ ,  $R_{71} = 10 \text{ }\Omega$ ,  $R_{72} = 10 \text{ }\Omega$ ,  $R_{73} = 10 \text{ }\Omega$ ,  $R_{74} = 10 \text{ }\Omega$ ,  $R_{75} = 10 \text{ }\Omega$ ,  $R_{76} = 10 \text{ }\Omega$ ,  $R_{77} = 10 \text{ }\Omega$ ,  $R_{78} = 10 \text{ }\Omega$ ,  $R_{79} = 10 \text{ }\Omega$ ,  $R_{80} = 10 \text{ }\Omega$ ,  $R_{81} = 10 \text{ }\Omega$ ,  $R_{82} = 10 \text{ }\Omega$ ,  $R_{83} = 10 \text{ }\Omega$ ,  $R_{84} = 10 \text{ }\Omega$ ,  $R_{85} = 10 \text{ }\Omega$ ,  $R_{86} = 10 \text{ }\Omega$ ,  $R_{87} = 10 \text{ }\Omega$ ,  $R_{88} = 10 \text{ }\Omega$ ,  $R_{89} = 10 \text{ }\Omega$ ,  $R_{90} = 10 \text{ }\Omega$ ,  $R_{91} = 10 \text{ }\Omega$ ,  $R_{92} = 10 \text{ }\Omega$ ,  $R_{93} = 10 \text{ }\Omega$ ,  $R_{94} = 10 \text{ }\Omega$ ,  $R_{95} = 10 \text{ }\Omega$ ,  $R_{96} = 10 \text{ }\Omega$ ,  $R_{97} = 10 \text{ }\Omega$ ,  $R_{98} = 10 \text{ }\Omega$ ,  $R_{99} = 10 \text{ }\Omega$ ,  $R_{100} = 10 \text{ }\Omega$ .

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Solution
\begin{align*} R_{\text{eq}} &= 132.8 \text{ }\Omega && \end{align*}
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Now a wye-delta transformation is necessary.

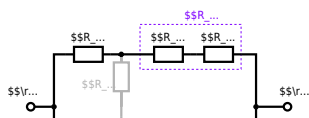


Since  $R_2=R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as: 
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series: 
$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{eq}$  between A and B.

Solution



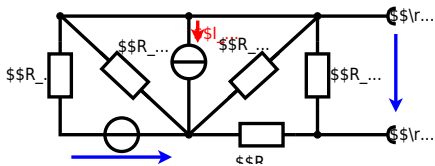
The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = (R_2 + R_1 + R_{-1}) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \Omega + 200 \Omega + 200 \Omega) \parallel (100 \Omega + 100 \Omega) \parallel R_{\text{eq}} = (500 \Omega) \parallel (200 \Omega) \parallel R_{\text{eq}} = \frac{500 \Omega \cdot 200 \Omega}{500 \Omega + 200 \Omega} \parallel$$

**Exercise E6 Equivalent linear Source  
(written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.  
Result

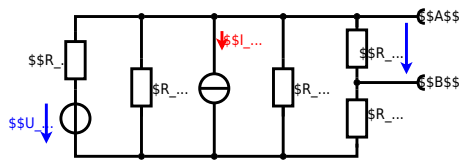
$$U_{\text{s}} = U_{\text{AB}} = 4.5 \text{ V} \quad R_{\text{i}} = R_{\text{AB}} = 6 \Omega$$



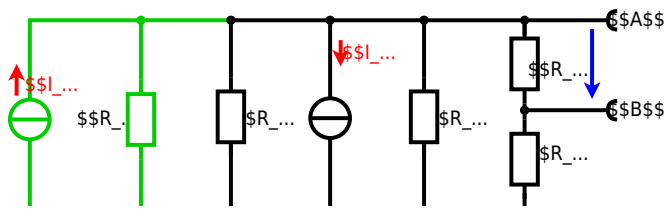
Calculated the internal resistance  $R_{\text{int}}$  and the source voltage  $U_{\text{oc}}$  of an equivalent linear voltage source on the connectors  $\text{A}$  and  $\text{B}$ .  $\begin{aligned} R_1 &= 5.0 \text{ } \Omega, & U_2 &= 6.0 \text{ V}, & R_3 &= 10 \text{ } \Omega, & I_4 &= 4.2 \text{ A}, & R_5 &= 10 \text{ } \Omega, & R_6 &= 7.5 \text{ } \Omega, & R_7 &= 15 \text{ } \Omega \end{aligned}$  Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in parallel, like also  $I_2$  and  $I_4$ : 
$$R_{135} = R_1 || R_3 || R_5$$
 
$$I_{24} = I_2 - I_4$$
 The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following: 
$$U_{24} = I_{24} \cdot R_{135} + U_2$$

$$U_{24} = U_{24} \cdot \left( \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) \cdot \left( \frac{R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \right)$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ .

Therefore the voltage between  $A$  and  $B$  is given as:

$$U_{AB} = U_{24} \cdot \left( \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right) \cdot \left( \frac{R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \right)$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0\Omega$ , so a short-circuit):

$$R_{AB} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with  $R_1 || R_3 || R_5 = 5\Omega || 10\Omega || 10\Omega = 5\Omega || 5\Omega = 2.5\Omega$ :

$$U_{AB} = \left( \frac{6.0\text{V}}{5.0\Omega} \right) \cdot 4.2\Omega \cdot \left( \frac{15\Omega \cdot 2.5\Omega}{7.5\Omega + 15\Omega + 2.5\Omega} \right)$$

$$R_{AB} = 15\Omega || (7.5\Omega + 2.5\Omega)$$

### Full Exam

These is the full exam

Full exam

#### Exercise E1 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)

The heating element made of nichrome wire with a cross-section of  $1.80\text{mm}^2$ . Each second, a power dissipation (= heat flow) of  $P=40\text{W}$  is necessary. Determine the current  $I$  needed to operate for heating elements. The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6}\Omega\text{m}$ . The heating element is  $3\text{m}$  long and has a diameter of  $3.57\text{mm}$ . Calculate the resistance  $R$  of the heating element.

Solution

$$P = U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} = \sqrt{\frac{40\text{W}}{0.33\Omega}}$$

$$R = \rho \cdot \frac{l}{A} \quad | \quad A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \quad | \quad R = \rho \cdot \frac{4 \cdot l}{d^2 \cdot \pi} \quad | \quad R = 1.10 \cdot 10^{-6}\Omega\text{m} \cdot \frac{4 \cdot 3\text{m}}{(3.57\text{mm})^2 \cdot \pi}$$

$$3 \cdot 10^{-3} \cdot (3.57 \cdot 10^{-3} \cdot R)^2 \cdot \pi$$

[electrical\\_engineering\\_and\\_electronics:task\\_rj0r6j4apumukrj6\\_with\\_calculation](#)  
[resistivity, power, exam ee1 ws2022](#)

**Exercise E2 Temperature-dependent Resistance**  
**(written test, approx. 6 % of a 60-minute written test, WS2022)**

A refrigerator is explained with the effect of temperature on the resistance of a resistor. The resistance of a resistor is given by  $R = R_0 (1 + \alpha \Delta T + \beta \Delta T^2)$  for  $R_0 = 65 \Omega$  at  $T_0 = 25^\circ\text{C}$ . Its temperature coefficients are:  $\alpha = 0.01 \text{ K}^{-1}$  and  $\beta = 71 \cdot 10^{-6} \text{ K}^{-2}$ .

The temperature inside the refrigeration system can reach down to  $-40^\circ\text{C}$ .

Result  
 Calculate the resistance of the thermistor at  $-40^\circ\text{C}$ .

The power transferred to the resistor  $P = U \cdot I$  and the heat  $Q = P \cdot t$  is solution for the resistive flow might heat up the refrigeration system. Therefore, with constant  $U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$R = R_0 (1 + \alpha \Delta T + \beta \Delta T^2) \quad | \text{with } \Delta T = T_{\text{end}} - T_{\text{start}}$$

$$R = 65 \Omega \cdot (1 + 0.01 \cdot (-40 - 25) + 71 \cdot 10^{-6} \cdot (-40 - 25)^2)$$

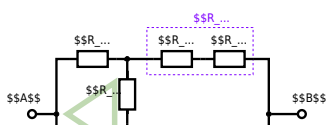
[electrical\\_engineering\\_and\\_electronics:task\\_70jg4yzznocarsq\\_with\\_calculation](#)  
[temperature dependent resistance, power, heat, exam ee1 ws2022](#)

**Exercise E4 Pure Resistor Network Simplification**  
**(written test, approx. 13 % of a 60-minute written test, WS2022)**

The following shall hold:  $R_1 = 20 \Omega$ ,  $R_2 = 10 \Omega$ ,  $R_3 = 10 \Omega$ ,  $R_4 = 10 \Omega$  and  $R_5 = 10 \Omega$ .  
 Result:  $R_{\text{in A}}$  and  $R_{\text{in B}}$ .

Solution  

$$R_{\text{in eq}} = 13.8 \Omega$$
  
 Now a wye-delta transformation is necessary.

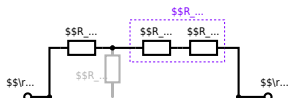


Since  $R_2=R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as: 
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \Omega)^2}{3 \cdot 100 \Omega} = \frac{1}{3} \cdot 100 \Omega = 33.33 \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series: 
$$R_{eq} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{eq} = 33.33 \Omega + (33.33 \Omega + 400 \Omega) \parallel (33.33 \Omega + 100 \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{eq}$  between  $A$  and  $B$ .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

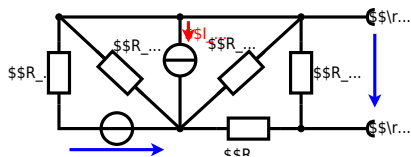
$$R_{\text{eq}} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel R_{\text{eq}} = (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel R_{\text{eq}} = (500 \, \Omega) \parallel (200 \, \Omega) \parallel R_{\text{eq}} = \frac{500 \, \Omega \cdot 200 \, \Omega}{500 \, \Omega + 200 \, \Omega}$$

[electrical\\_engineering\\_and\\_electronics:task\\_x357drkaqv84jnsc\\_with\\_calculation\\_network\\_simplification,\\_exam\\_ee1\\_ws2022](#)

**Exercise E6 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)**

The circuit in the following has to be simplified.  
Result

$$U_{\text{S}} = U_{\text{AB}} = 4.5 \, \text{V} \parallel R_{\text{i}} = R_{\text{AB}} = 6 \, \Omega$$



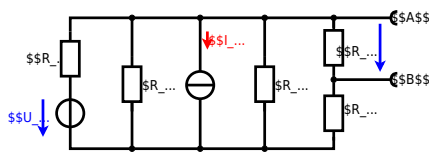
Calculate the internal resistance  $R_i$  and the source voltage  $U_s$  of an equivalent linear voltage source on the connectors A and B.

$R_1=5.0 \text{ } \Omega$ ,  $U_1=6.0 \text{ V}$ ,  $R_2=10 \text{ } \Omega$ ,  $I_1=4.2 \text{ A}$ ,  
 $R_3=10 \text{ } \Omega$ ,  $R_4=7.5 \text{ } \Omega$ ,  $R_5=15 \text{ } \Omega$

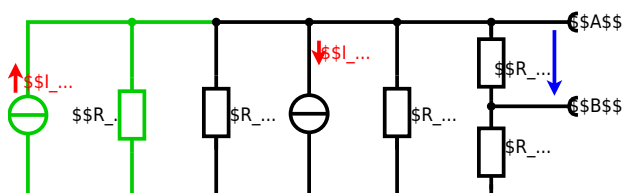
Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:

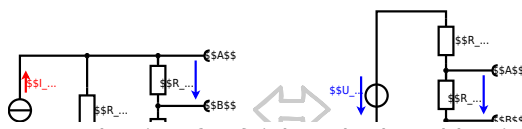


The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in

parallel, like also  $I_2$  and  $I_4$ : 
$$R_{135} = R_1 || R_3 || R_5$$
 
$$I_{24} = I_2 - I_4 = \left\{ \frac{U_2}{R_1} \right\} - I_4$$
 The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following: 
$$U_{24} = R_{135} \cdot I_{24} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot R_1 || R_3 || R_5$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ . Therefore the voltage between  $A$  and  $B$  is given as: 
$$U_{\text{AB}} = U_{24} \cdot \left\{ \frac{R_7}{R_6 + R_7 + R_1 || R_3 || R_5} \right\} = \left( \frac{U_2}{R_1} - I_4 \right) \cdot \left\{ \frac{R_7 \cdot R_1 || R_3 || R_5}{R_6 + R_7 + R_1 || R_3 || R_5} \right\}$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $=0\Omega$ , so a short-circuit): 
$$R_{\text{AB}} = R_7 || (R_6 + R_1 || R_3 || R_5)$$

with  $R_1 || R_3 || R_5 = 5 \Omega || 10 \Omega || 10 \Omega = 5 \Omega || 5 \Omega = 2.5 \Omega$ :

$$U_{\text{AB}} = \left\{ \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \right\} \cdot \left\{ \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \right\}$$

$$R_{\text{AB}} = 15 \Omega || (7.5 \Omega + 2.5 \Omega)$$

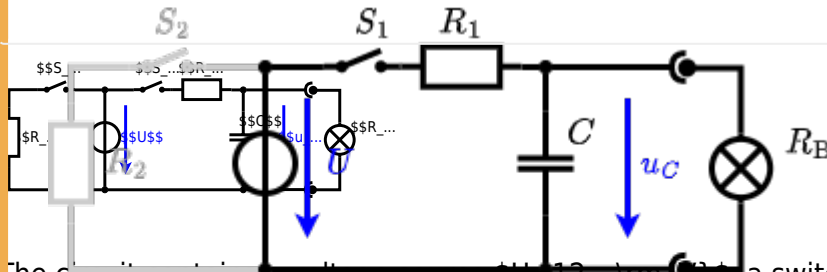
[electrical\\_engineering\\_and\\_electronics:task\\_6tqtqtue1e2nf2c7\\_with\\_calculation](#)  
 dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

### Exercise E8 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)

The capacitor becomes fully charged (voltage across the capacitor is  $U$ ) again. The voltage across the capacitor is again  $0$  V at the moment  $t_0=0$  s when the switch  $S_1$  is closed. Calculate the voltage  $u_c(t_2)$  across the capacitor at  $t_2=1$  ms after closing the switch.

Hint: To solve this, first create an equivalent linear voltage source from  $U$ ,  $R_1$ , and  $R_B$ .

The internal voltage source is  $U_{int} = U \cdot \frac{R_B}{R_1 + R_B}$  and the internal resistance is  $R_{int} = R_1 \parallel R_B = \frac{R_1 \cdot R_B}{R_1 + R_B}$ .  
 On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting  $R_2$ .



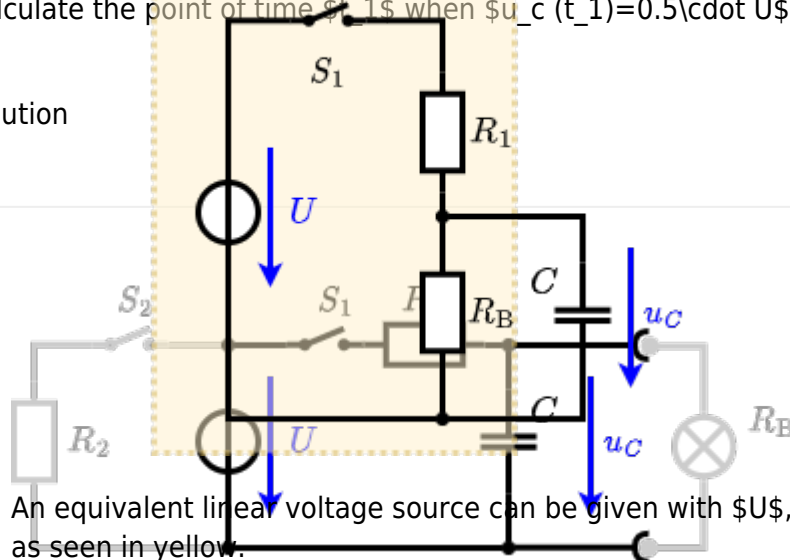
The circuit contains a voltage source  $U=12$  V, a switch  $S_1$ , a resistor of  $R_1=20$   $\Omega$  and a capacitor of  $C=100$   $\mu$ F.

The switch  $S_2$  to an additional consumer  $R_2$  will be considered to be open for the first tasks. At the moment  $t_0=0$  s the switch  $S_1$  is closed, the voltage across the capacitor is  $u_c(t_0)=0$  V.

First do not consider the light bulb - it is not connected to the RC circuit.

Calculate the point of time  $t_1$  when  $u_c(t_1)=0.5 \cdot U$ .

Solution



An equivalent linear voltage source can be given with  $U$ ,  $R_1$ , and  $R_B$  as seen in yellow.

Therefore, the voltage of the equivalent instant source is  $U_{int} = U \cdot \frac{R_B}{R_1 + R_B} = 1/2 \cdot U$ . The internal resistance is given by  $R_{int} = R_1 \parallel R_B = \frac{R_1 \cdot R_B}{R_1 + R_B}$ .

The following formula describes the time course of  $u_c(t)$  which has to be  $u_c(t) = U_{int} \cdot (1 - e^{-t/\tau})$  with  $\tau = R_{int} \cdot C$ . It has to be rearranged to  $(1 - e^{-t/\tau}) = 0.5 \cdot U$   
 $e^{-t/\tau} = 0.5$   
 $-\frac{t}{\tau} = \ln(0.5)$   
 $t = -\tau \cdot \ln(0.5) = R_1 \cdot C \cdot \ln(2)$



**(written test, approx. 18 % of a 60-minute written test, WS2022)**

2. A series circuit contains a resistor with  $R = 100 \Omega$  and a capacitor with  $C = 40 \text{ nF}$ . The voltage across the resistor is  $U_R = 100 \text{ V}$  and the voltage across the capacitor is  $U_C = 40 \text{ V}$ . The current through the circuit is  $I = 1 \text{ A}$ . Calculate the total impedance  $Z$  and the total voltage  $U$  across the series circuit.

Solution

$$Z = \sqrt{R^2 + X_C^2} = \sqrt{100^2 + (1/(2\pi \cdot 40 \cdot 10^{-9}))^2} = 100 \Omega$$

$$U = I \cdot Z = 1 \text{ A} \cdot 100 \Omega = 100 \text{ V}$$

Result

A series circuit means that the current is constant on every component. The equivalent impedance for  $R$  and  $X_C$  combined is given by  $Z = \sqrt{R^2 + X_C^2}$ . Parallel circuit means that the voltage is the same on  $R$  and  $X_C$ .  $U_R = U_C = U$ .  $I = U/Z$ .  $Z = \sqrt{R^2 + X_C^2}$ .  $X_C = 1/(2\pi \cdot f \cdot C)$ .  $f = 150 \text{ kHz}$ .  $C = 40 \text{ nF}$ .  $R = 100 \Omega$ .  $U_R = 100 \text{ V}$ .  $U_C = 40 \text{ V}$ .  $I = 1 \text{ A}$ .  $Z = \sqrt{100^2 + (1/(2\pi \cdot 150 \cdot 10^3 \cdot 40 \cdot 10^{-9}))^2} = 100 \Omega$ .  $U = I \cdot Z = 1 \text{ A} \cdot 100 \Omega = 100 \text{ V}$ .  $Z = 100 \Omega$ .  $U = 100 \text{ V}$ .

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[complex impedance, exam ee1 ws2022](#)

**Exercise E14 Complex Impedance Circuit**

**(written test, approx. 15 % of a 60-minute written test, WS2022)**

1. Calculate the effective value  $I_{eff}$  for a series circuit with  $R = 10 \Omega$ ,  $C = 10 \mu\text{F}$  and  $L = 1 \text{ mH}$ . The voltage source is  $u(t) = 3.0 \text{ V} \cdot \sin(2\pi \cdot 15 \text{ kHz} \cdot t)$ . The circuit is connected with an inductor of  $L = 330 \mu\text{H}$  and a capacitor of  $C = 0.22 \mu\text{F}$ , all in series.

Solution

Result

$$Z = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{10^2 + (2\pi \cdot 15 \cdot 10^3 \cdot 330 \cdot 10^{-6} - 1/(2\pi \cdot 15 \cdot 10^3 \cdot 0.22 \cdot 10^{-6}))^2} = 48.2 \Omega$$

$$I_{eff} = U_{eff} / Z = 3.0 \text{ V} / 48.2 \Omega = 0.062 \text{ A} = 62 \text{ mA}$$

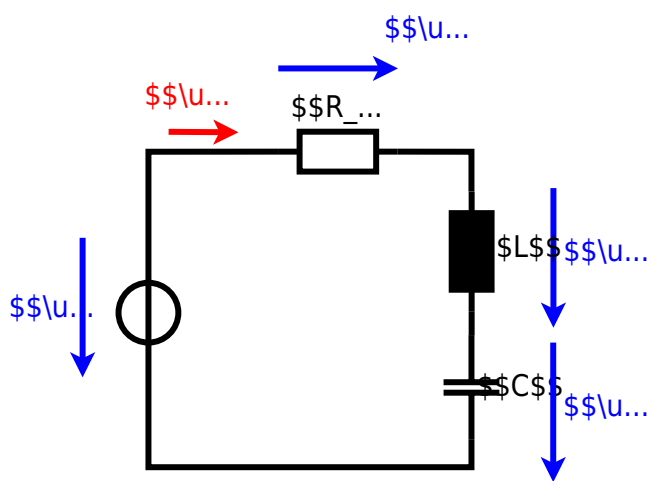
Draw the circuit diagram of the given circuit. Label the components, voltages, and currents.

$$Z = \sqrt{R^2 + (X_L - X_C)^2} = \sqrt{10^2 + (2\pi \cdot 15 \cdot 10^3 \cdot 330 \cdot 10^{-6} - 1/(2\pi \cdot 15 \cdot 10^3 \cdot 0.22 \cdot 10^{-6}))^2} = 48.2 \Omega$$

$$I_{eff} = U_{eff} / Z = 3.0 \text{ V} / 48.2 \Omega = 0.062 \text{ A} = 62 \text{ mA}$$







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