

task_7el8zljglaazxtw_with_calculation

Student Group

First Name	Surname	Matrikel Nr.

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resonant circuit, exam ee2 SS2022

Exercise E13 Series Resonant Circuit**(written test, approx. 10 % of a 120-minute written test, SS2022)**

2. What is the resonance frequency of the circuit shown in the circuit diagram? The circuit diagram shows a series resonant circuit with a voltage source U , a resistor R , an inductor L , and a capacitor C .

At resonance, the inductive reactance X_L and the capacitive reactance X_C are equal in magnitude and cancel each other out. The total impedance Z_{RLC} is then purely resistive and equal to the resistance R .

Path: $C = 10 \text{ nF}$

$$R = 88.6 \text{ m}\Omega$$

Path: $L = 60 \text{ nH}$

$$R = 88.6 \text{ m}\Omega$$

The resonance frequency is given as

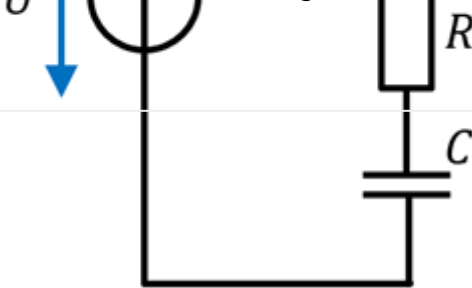
$$f_0 = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{60 \cdot 10^{-12} \cdot 10 \cdot 10^{-9}}} = 205.5 \text{ MHz}$$

What is the total impedance Z_{RLC} at resonance? The total impedance is purely resistive and equal to the resistance R .

$$Z_{RLC} = R = 88.6 \text{ m}\Omega$$

At resonance, the impedance is purely resistive.

$$\text{With values: } C = 10 \text{ nF} = 10 \cdot 10^{-9} \text{ F} \quad L = 60 \text{ nH} = 60 \cdot 10^{-9} \text{ H}$$



1. What is the impedance $\underline{Z}_{RLC}$ of this real capacitor for $f_0 = 100 \text{ MHz}$? (Phase and magnitude)

Path

The impedance $\underline{Z}_{RLC}$ is given by:

$$\underline{Z}_{RLC} = R + j\omega L - \frac{j}{\omega C} = R + j\left(\omega L - \frac{1}{\omega C}\right)$$

Putting in the numbers, only for the reactive part X_{LC} :

$$X_{LC} = 2\pi \cdot 100 \cdot 10^6 \cdot 60 \cdot 10^{-9} - \frac{1}{2\pi \cdot 100 \cdot 10^6 \cdot 10 \cdot 10^{-9}} = 121.45 \text{ m}\Omega$$

With the real and imaginary parts, we can derive the magnitude and phase:

$$\begin{aligned} Z_{\text{RLC}} &= \sqrt{R^2 + X_{\text{LC}}^2} \quad \&= \sqrt{(88 \text{ m}\Omega)^2 + (-121.45 \text{ m}\Omega)^2} \quad \&= 150.0... \text{ m}\Omega \\ \end{aligned}$$

$$\begin{aligned} \varphi &= \arctan \left(\frac{X_{\text{LC}}}{R} \right) \quad \&= \arctan \left(\frac{-121.45 \text{ m}\Omega}{88 \text{ m}\Omega} \right) \quad \&= -0.9437... \\ &= -54.07...^\circ \quad \end{aligned}$$

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Last update: **2024/07/05 02:21**

