

task_elndbo3xwi2klxuu_with_calculation

Student Group

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Exercise E15 Lorentz Force (hard!)

(written test, approx. 10 % of a 120-minute written test, SS2021)

A) The picture on the right shows a straight high voltage direct current transmission line with a length of $l = 1200 \text{ m}$. The resulting force is? (Independent)

A homogeneous geomagnetic field is assumed. The magnetic field strength has a vertical component of $B_{\text{v}} = 40 \text{ } \mu\text{T}$ and a horizontal component of $B_{\text{h}} = 20 \text{ } \mu\text{T}$.

The angle between the transmission line and the horizontal component of the field strength is $\alpha = 20^\circ$.

The picture on the right shows the line (black), the field strength components, and the angle in front and top view for illustration purposes.

Top View

Path

a)

Calculate the force that results from the current flow on the entire conductor.

First, calculate the vertical and horizontal components and combine them accordingly.

Path

- The horizontal component $\vec{F}_{\text{h}}$ of the force is based on the vertical component $\vec{B}_{\text{v}}$ of the magnetic field.
- The vertical component $\vec{B}_{\text{v}}$ of the magnetic field is not shown in the image but is pointing into the ground.

It has to be perpendicular to $\vec{B}_{\text{v}}$ and to $\vec{I}$. The right-hand rule has to be applied.

$$\vec{F} = I \cdot (\vec{I} \times \vec{B})$$

\end{align*}

Here, we have two components for the current - and therefore for the force - to evaluate.

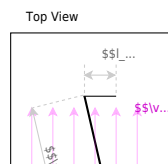
Considering the right-hand rule (and the cross product), the vertical field B_{v} generates a horizontal force F_{h} and vice versa.

The **horizontal component** is given by

$$\begin{aligned} F_{\text{h}} &= I \cdot (I \cdot B_{\text{v}}) \quad \&= 1'200 \text{ } \sim \text{A} \cdot 300 \\ &\cdot 10^3 \text{ } \sim \text{m} \cdot 40 \cdot 10^{-6} \text{ } \sim \left\{ \frac{\text{Vs}}{\text{m}^2} \right\} \quad \&= 14'400 \\ &\sim \left\{ \frac{\text{VAs}}{\text{m}} \right\} = 14'400 \sim \left\{ \frac{\text{Ws}}{\text{m}} \right\} = 14'400 \sim \text{N} \end{aligned}$$

For the **vertical component** the angle α has to be considered.

For the maximum $F_{\rm v}$ the angle α has to be 90° , therefore the $\sin$ has to be used.



$$F_v = I \cdot l \cdot B_h \cdot \sin \alpha \quad \&= 1'200$$

$$\{ \sim \text{A} \} \cdot 300 \cdot 10^3 \{ \sim \text{m} \} \cdot 40 \cdot 10^{-6} \{ \sim \text{Vs} \} \over {m^2} \} \cdot \sin 20^\circ \quad \&= 2'462.545... \sim \text{N} \end{align*}$$

For the **overall force** F the Pythagorean theorem has to be used:

$$\begin{aligned} F &= \sqrt{F_v^2 + F_h^2} \quad \&= \sqrt{(14'400 \sim \text{rm N})^2 + (2'462.545... \sim \text{rm N})^2} \quad \&= 14'609.04... \sim \text{rm N} \end{aligned}$$

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Last update: **2024/07/03 15:21**

