

task_wjttvmydrskzhcim_with_calculation

Student Group

First Name	Surname	Matrikel Nr.

Table of Contents

Exercise E20 Component Parameters (written test, approx. 10 % of a 120-minute written test, SS2021)	2
---	---

complex voltage divider, RMS, inductor, exam ee2 SS2021

Exercise E20 Component Parameters**(written test, approx. 10 % of a 120-minute written test, SS2021)**

Determine the component parameters of a motor (motor M) presents a resistive inductive load! For the next exercises consider the following: The RMS values of the series resistance R_{M} and the inductance L_{M} are to be determined below. Both results in the impedance of the motor. But two different frequencies, f_1 and f_2 was applied.

This resulted in the recorded current of

a) Derive in general the equation for the absolute value of the impedance of the motor.

$$|Z| = \sqrt{(2\pi \cdot f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

$$R_{\text{M}} = 4 \cdot \Omega$$

$$L_{\text{M}} = 100 \cdot \text{mH}$$

b) Since we have the absolute values of the impedances from the specified formulas from a) and b) this has the advantage that R_{M} will cancel out: $Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - ((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2)$

The complex impedance \underline{Z} for a resistive inductive load R_{M} and L_{M} in series circuit is given as $\underline{Z} = R_{\text{M}} + jX_L$

$$\underline{Z} = R_{\text{M}} + j \cdot 2\pi \cdot f \cdot L_{\text{M}}$$

Now we can rearrange to L_{M} :

The Pythagorean theorem can derive the absolute value:

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - ((2\pi \cdot f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2)$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 - (2\pi \cdot f_1 \cdot L_{\text{M}})^2$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi \cdot L_{\text{M}})^2 (f_2^2 - f_1^2)$$

$$L_{\text{M}} = \frac{|Z_2|^2 - |Z_1|^2}{(2\pi)^2 (f_2^2 - f_1^2)}$$

And then to L_{M} :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{|Z_2|^2 - |Z_1|^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10 \cdot \Omega)^2 - (6.25 \cdot \Omega)^2}{(100 \cdot \text{s}^{-1})^2 - (50 \cdot \text{s}^{-1})^2}}$$

$$= 14.346... \cdot \text{mH}$$

The resistance value R_{M} can be derived from $Z_2^2 = (2\pi \cdot f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2$

$$R_{\text{M}}^2 = Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2$$

$$R_{\text{M}} = \sqrt{Z_2^2 - (2\pi \cdot f_2 \cdot L_{\text{M}})^2}$$

The values have to be inserted also for R_{M} :

$$R_{\text{M}} = \sqrt{(10 \cdot \Omega)^2 - (2\pi \cdot 100 \cdot \text{s}^{-1} \cdot 0.014346... \cdot \text{H})^2}$$

$$= 4.3301... \cdot \Omega$$

From:

<https://first.mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:

https://first.mexle.te.hs-heilbronn.de/ee2/task_wjttvmydrskzhcim_with_calculation

Last update: **2024/07/04 01:51**

