

task_wjttvmydrskzhcim_with_calculation

Student Group

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complex voltage divider, RMS, inductor, exam ee2 SS2021

Exercise E1 Component Parameters**(written test, approx. 10 % of a 120-minute written test, SS2021)**

For the next exercises consider the following circuit. The motor presents a resistive inductive load!

Results of the series measurements, an AC voltage with a constant RMS value of $U_{\text{RMS}} = 50 \text{ V}$ but two different frequencies, f_1 and f_2 was applied.

This resulted in the recorded current of

a) Derive in general the equation for the absolute value of the impedance of the motor.

$$|Z| = \sqrt{(2\pi f \cdot L_{\text{M}})^2 + R_{\text{M}}^2}$$

$$R_{\text{M}} = 4.3301 \text{ } \Omega$$

$$L_{\text{M}} = 14.346 \text{ mH}$$

b) Since we have $|Z_1|$ and $|Z_2|$ from b) we can subtract two of the formulas from a). This has the advantage that R_{M} will cancel out:

$$|Z_2|^2 - |Z_1|^2 = (2\pi f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2 - ((2\pi f_1 \cdot L_{\text{M}})^2 + R_{\text{M}}^2)$$

$$|Z_2|^2 - |Z_1|^2 = (2\pi)^2 \cdot L_{\text{M}}^2 \cdot (f_2^2 - f_1^2)$$

The complex impedance $\underline{Z}$ for a resistive inductive load $R_{\text{M}} + j\omega L_{\text{M}}$ in a series circuit is given as

$$\underline{Z} = R_{\text{M}} + j\omega L_{\text{M}}$$

Now we can rearrange to L_{M} :

$$L_{\text{M}} = \frac{|Z_2|^2 - |Z_1|^2}{(2\pi)^2 \cdot (f_2^2 - f_1^2)}$$

$$L_{\text{M}} = \frac{(50 \text{ V})^2 - (50 \text{ V})^2}{(2\pi)^2 \cdot (100 \text{ Hz})^2 - (50 \text{ Hz})^2}$$

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And then to L_{M} :

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{|Z_2|^2 - |Z_1|^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_{\text{M}} = \frac{1}{2\pi} \sqrt{\frac{(10 \text{ V})^2 - (6.25 \text{ V})^2}{(100 \text{ Hz})^2 - (50 \text{ Hz})^2}} = 14.346 \text{ mH}$$

The resistance value R_{M} can be derived from $|Z_2|^2 = (2\pi f_2 \cdot L_{\text{M}})^2 + R_{\text{M}}^2$

$$R_{\text{M}} = \sqrt{(10 \text{ V})^2 - (2\pi \cdot 100 \text{ Hz} \cdot 14.346 \text{ mH})^2} = 4.3301 \text{ } \Omega$$

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