

Block 01 — Physical Quantities and SI System

Student Group

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Block 01 — Physical quantities and SI system

Learning objectives

- Use the SI base quantities, units, and symbols correctly; convert between units with prefixes.
- Distinguish base vs. derived quantities; express key EE units (e.g. V , V , V) in SI base units.
- Apply quantity equations and perform unit (dimensional) checks; contrast with normalized (dimensionless) equations.
- Read and use common Latin/Greek letter symbols; distinguish uppercase/lowercase and instantaneous vs. constant quantities.

90-minute plan

1. Warm-up (10 min):
 1. “What is the unit of conductivity? of energy?”
2. Quick prefix quiz; everyday magnitude estimates (mA , $\text{k}\Omega$, μF).
3. Core concepts & derivations (60 min):
 1. SI base set $\rightarrow$ derived units; prefix rules;
4. quantity vs. normalized equations;
5. dimensional checks.
 1. Prefix ladder ($\text{E}\dots\text{a}$) and best-practice rounding/checks.
 2. Symbols & Greek letters in EE1; time-varying vs constant symbols.
6. Practice (15 min): Fast conversions and unit checks (individual $\rightarrow$ pair).
7. Wrap-up (5 min): Summary table; common pitfalls checklist.

Conceptual overview

1. Units are the grammar of engineering and physics.
2. The SI defines seven **base quantities** and units; all other (derived) units are built from these without extra numerical factors. The SI defines seven **base quantities** and units.
3. In EE1 we work strictly in the SI system, combining **numerical value $\times$ unit** and tracking dimensions at every step (e.g., $I=2\sim\text{A}$ means “two times one ampere”).
4. Derived units (e.g., V , Ω , S) must reduce to base units without hidden factors.
5. **Prefixes** scale units by powers of ten to keep numbers readable. Prefixes compress very large and very small numbers so we can compute and compare safely.
6. **Quantity equations** keep units; **normalized equations** cancel units to yield dimensionless ratios (e.g., efficiency).
7. In EE, symbol choices and letter case matter: U vs. $u(t)$, M (mega) vs. m (milli). We adopt a consistent symbol set (Latin + Greek), and distinguish **constants** (capital letters) from **time functions** (lowercase, e.g., $u(t)$).
8. Finally, we preview the three anchor quantities for the next blocks: **charge** (what moves), **current** (how fast charge moves), and **voltage** (energy per charge). Physics describes **quantities** with a **numerical value $\times$ unit** (e.g., $I=2\sim\text{A}$).

SI base quantities and units

- For practical applications of physical laws of nature, **physical quantities** are put into mathematical relationships.
- There are basic quantities based on the SI system of units (French for *Système International d'Unités*), see below.
- In order to determine the basic quantities quantitatively (quantum = Latin for *how big*), **physical units** are defined, e.g. m for length.
- In electrical engineering, the first three basic quantities (cf. [table 1](#)) are particularly important.
Mass is important for the representation of energy and power.
- Each physical quantity is indicated by a product of **numerical value** and **unit**:
e.g. $I = 2 \text{ A}$
 - This is the short form of $I = 2 \cdot 1 \text{ A}$
 - I is the physical quantity, here: electric current strength
 - 2 is the numerical value
 - A is the (measurement) unit, here: Ampere

Base quantity	Name	Unit	Definition
Time	Second	s	Oscillation of ^{133}Cs -Atom
Length	Meter	m	by speed of light
el. Current	Ampere	A	by elementary charge
Mass	Kilogram	kg	still by kg prototype
Temperature	Kelvin	K	by triple point of water
amount of substance	Mol	mol	via number of ^{12}C nuclides
luminous intensity	Candela	cd	via given radiant intensity

Tab. 1: SI base quantities (SI)

Common derived quantities

- Besides the basic quantities, there are also quantities derived from them, e.g. $[F] = [\text{m}] \cdot [\text{a}] \rightarrow 1 \text{ N} = 1 \text{ kg} \cdot \frac{1 \text{ m}}{1 \text{ s}^2}$.
- SI units should be preferred for calculations. These can be derived from the basic quantities **without a numerical factor**.
example:
 - The pressure unit bar (bar) is an SI unit.
 - BUT: The obsolete pressure unit "Standard atmosphere" ($= 1.013 \text{ bar}$) is **not** an SI unit.
- To prevent the numerical value from becoming too large or too small, it is possible to replace a decimal factor with a prefix. These are listed in [table ##](#).

We will see, that a lot of electrical quantities are derived quantities.

Prefixes

- Use prefixes to keep magnitudes practical

- (see [table 2](#) and [table 3](#)).
- Instead of writing zeroes for like in $0.000000004 \text{ ~}\mathrm{C}$ it is easier to write $4 \text{ ~}\mathrm{nC}$.
 - For calculation it is often easier to write $4 \text{ ~}\mathrm{nC} = 4 \cdot 10^{-9} \text{ ~}\mathrm{C}$ or the notation 4e-9 C

Physical equations

- Physical equations allow a connection of physical quantities.
- There are two types of physical equations to distinguish:
 - Quantity equations (in German: *Größengleichungen*)
 - Normalized quantity equations (also called related quantity equations, in German *normierte Größengleichungen*)

Quantity Equations

The vast majority of physical equations result in a physical unit that does not equal 1 .

Example: Force $F = m \cdot a$ with $[F] = 1 \text{ ~}\mathrm{kg} \cdot \frac{\text{m}}{\text{s}^2}$

- A unit check should always be performed for quantity equations

normalized Quantity Equations

In normalized quantity equations, the measured value or calculated value of a quantity equation is divided by a reference value. This results in a dimensionless quantity relative to the reference value.

Example: The efficiency $\eta = \frac{P_{\text{O}}}{P_{\text{I}}}$ is given as quotient between the outgoing power P_{O}

prefix	prefix symbol	meaning
Yotta	Y	10^{24}
Zetta	Z	10^{21}
Exa	E	10^{18}
Peta	P	10^{15}
Tera	T	10^{12}
Giga	G	10^9
Mega	M	10^6
Kilo	k	10^3
Hecto	h	10^2
Deka	de	10^1

Tab. 2: Prefixes I

prefix	prefix symbol	meaning
Deci	d	10^{-1}
Centi	c	10^{-2}
Milli	m	10^{-3}
Micro	$\mathrm{\mu}$, μ	10^{-6}
Nano	n	10^{-9}
Piko	p	10^{-12}
Femto	f	10^{-15}
Atto	a	10^{-18}
Zeppto	z	10^{-21}
Yocto	y	10^{-24}

Tab. 3: Prefixes II

- Quantity equations should generally be preferred

P_{I} and the incoming power P_{I} .

As a reference the following values are often used:

- Nominal values (maximum permissible value in continuous operation) or
- Maximum values (maximum value achievable in the short term)

For normalized quantity equations, the units should **always** cancel out.

Letters for physical quantities

Latin/Greek letters are reused across physics.

In physics and electrical engineering, the letters for physical quantities are often close to the English term.

Thus explains C for **C**apacity, Q for **Q**uantity and ϵ_0 for the **E**lectrical Field Constant. But, maybe you already know that C is used for the thermal capacity as well as for the electrical capacity. The Latin alphabet does not have enough letters to avoid conflicts for the scope of physics. For this reason, Greek letters are used for various physical quantities (see [table 4](#)).

Uppercase letters	Lowercase letters	Name	Application
A	α	Alpha	angles, linear temperature coefficient
B	β	Beta	angles, quadratic temperature coefficient, current gain
Γ	γ	Gamma	angles
Δ	δ	Delta	small deviation, length of a air gap

Especially in electrical engineering, **upper/lower case letters** are used to distinguish between

- a constant (time-independent) quantity, e.g. the period T
- or a time-dependent quantity, e.g. the instantaneous voltage $u(t)$
- EE relies on case and context (e.g., U vs. $u(t)$). Time-varying quantities often use lowercase, constants uppercase.

Notation & units

The course consistently uses the following symbols, units, and typical values:

Symbol	Quantity	SI unit	name of the unit	Typical values
q	Electric charge	C	Coulomb	10^{-19} C (electron) to mC
I	Electric current	A	Ampere	μA (sensors) to kA (lightning)
U	Voltage (potential difference)	V	Volt	μV (noise) to MV (transmission lines)
φ	Electric potential	V	Volt	—
P	Power	W	Watt	mW (electronics) to MW (machines)
W	Energy	J	Joule	μJ (capacitors) to MJ (batteries)
R	Resistance	Ω	Ohm	$\text{m}\Omega$ to $\text{M}\Omega$
G	Conductance	S	Siemens	μS to S
ρ	Resistivity	$\Omega\cdot\text{m}$	—	$1.7\cdot 10^{-8}$ $\Omega\cdot\text{m}$ (Cu)
σ	Conductivity	S/m	—	$5.8\cdot 10^7$ S/m (Cu)

Uppercase letters	Lowercase letters	Name	Application
E	ϵ, ε	Epsilon	electrical field constant, permittivity
Z	ζ	Zeta	- (math function)
H	η	Eta	efficiency
Θ	θ, ϑ	Theta	temperature in Kelvin
I	ι	Iota	-
K	κ	Kappa	specific conductivity
Λ	λ	Lambda	- (wavelength)
M	μ	Mu	magnetic field constant, permeability
N	ν	Nu	-
Ξ	ξ	Xi	-
O	$\omicron$	Omicron	-
Π	π	Pi	math. product operator, math. constant
R	ρ, ϱ	Rho	specific resistivity
Σ	σ	Sigma	math. sum operator, alternatively for specific conductivity
T	τ	Tau	time constant
Υ	υ	Upsilon	-
Φ	ϕ, φ	Phi	magnetic flux, angle, potential
X	χ	Chi	-
Ψ	ψ	Psi	linked magnetic flux
Ω	ω	Omega	unit of resistance, angular frequency

Tab. 4: greek letters

Symbol	Quantity	SI unit	name of the unit	Typical values
C	Capacitance	F	Farad	μF (ceramic) to F (supercaps)
L	Inductance	H	Henry	μH to H
E	Electric field strength	V/m	—	$1 \sim 10^6 V/m$ to $10^8 V/m$ (breakdown)
D	Electric flux density	C/m^2	—	—
B	Magnetic flux density	T	Tesla	μT (Earth) to several T (MRI)
H	Magnetic field strength	A/m	—	—
Φ	Magnetic flux	Wb	Weber	μWb to mWb
θ	magnetic voltage (Magnetomotive force)	$A \cdot \text{turn}$	—	—
R	Reluctance	A/Wb	—	—

Tab. 5: Course-wide notation and units

Common pitfalls & misconceptions

- **Case matters:** M (mega, 10^6) vs. m (milli, 10^{-3});
- **Micro symbol:** use μ (or u only when typing constraints exist);
- **usage of prefixes** never stack prefixes (no “ $m\mu F$ ”).
- **Mixed units:** keep SI consistently; avoid mixing h (hours) inside SI derivations.
- **Units vs. variables:** don't confuse W (work) with W (Watt = unit of power P = work per second).
Don't confuse C (capacity = charge per voltage) with C (Coulomb = unit of charge Q).
- **Units vs. prefixes:** don't confuse mN (Millinewton) with Nm (Newton meter).
- **Normalized vs. quantity equations:** dimensionless ratios should cancel units; if not, something's wrong.

Exercises

Worked example(s)

1) Unit check (quantity equation): Show that $P = U \cdot I$ has unit watt.

1. $[U] = \text{V} = \text{kg} \cdot \text{m}^2 \cdot \text{s}^{-3} \cdot \text{A}^{-1}$, $[I] = \text{A}$.
2. $[P] = [U][I] = \text{kg} \cdot \text{m}^2 \cdot \text{s}^{-3} = \text{W}$.

2) Prefix conversion: $3.3~\text{mA} = 3.3 \times 10^{-3}~\text{A} = 3300~\mu\text{A}$.

3) Work from lifting (quantity equation): $W = mgs$ with
 $m = 100~\text{kg}$, $g = 9.81~\text{m/s}^2$, $s = 2~\text{m}$.
 $W = 100 \cdot 9.81 \cdot 2~\text{Nm} = 1962~\text{J}$.

Quick checks

Exercise E1.1 Conversion

Convert $47~\text{k}\Omega$ to $\text{M}\Omega$ and Ω .

Result

$47~\text{k}\Omega = 0.047~\text{M}\Omega = 47\,000~\Omega$.

Exercise E2.2 Dimension

Is $\eta = \frac{P_{\text{O}}}{P_{\text{I}}}$ dimensionless?

Result

Yes. Units cancel (W/W); normalized equation.

Exercise E3.3 Conversion

Which is larger: $5~\text{mA}$ or $4500~\mu\text{A}$?

Result

$5\text{ mA} = 5000\text{ }\mu\text{A}$, so 5 mA is larger.

Exercise E4.4 Conversion

True/False: $1\text{ V} = 1\text{ Nm/As}$.

Result

True (from $W = U \cdot Q$).

Longer exercises

Exercise E1 Conversions: Battery

2. How many minutes could a car battery with 10 kWh of energy supplied by provided to a given power for the calculated time?

Result

$t = 200'000\text{ min}$

There are additional losses:

$W = 10\text{ kWh} = 10'000\text{ Wh}$ $t = \frac{W}{P}$
 • The battery has an internal resistance. Depending on the current the battery provides, this leads to internal losses.

- The internal resistance of the battery depends on the state of charge (SoC) of the battery.
- The wires also add additional losses to the system.

Exercise E7 Conversions: Speed, Energy, and Power

2. The energy of a 600 g fly is about $1.6 \cdot 10^{-19} \text{ J}$. How much energy does a 1 kg fly have? (1 kg = 1000 g)
3. A vehicle speed of $80 \frac{\text{km}}{\text{h}}$ in $\frac{\text{m}}{\text{s}}$

Solution

Fast Solution:

$$\begin{aligned} 1 \text{ kg} &= 1000 \text{ g} \\ 1.6 \cdot 10^{-19} \text{ J/g} &\cdot 1000 \text{ g/kg} = 1.6 \cdot 10^{-16} \text{ J/kg} \\ 1 \text{ kg} &\cdot 1.6 \cdot 10^{-16} \text{ J/kg} = 1.6 \cdot 10^{-16} \text{ J} \end{aligned}$$

$$\begin{aligned} 80 \frac{\text{km}}{\text{h}} &= 80 \cdot \frac{1000 \text{ m}}{3600 \text{ s}} = 22.22 \frac{\text{m}}{\text{s}} \\ 22.22 \frac{\text{m}}{\text{s}} &= 22.22 \frac{\text{m}}{\text{s}} \cdot \frac{3600 \text{ s}}{3600 \text{ s}} = 80 \frac{\text{km}}{\text{h}} \end{aligned}$$

Exercise E8 Conversion: Vacuum Cleaner

Your 18 V vacuum cleaner is equipped with a 4.0 Ah battery, it runs 15 minutes .

How much electrical power is consumed by the motor during this time on average?

Solution:

$$288 \text{ W}$$

$$\begin{aligned} W &= 18 \text{ V} \cdot 4.0 \text{ Ah} = 72 \text{ Wh} \\ 15 \text{ min} &= 0.25 \text{ h} \\ P &= \frac{W}{t} = \frac{72 \text{ Wh}}{0.25 \text{ h}} = 288 \text{ W} \end{aligned}$$

Exercise E9 Conversions: Video on Prefixes



Exercise E10 Conversion: Energy Consumption

Convert the following values step by step:

Result

How much energy does an average household consume per day when consuming an average power of 500 W ?

How many chocolate bars ($2'000 \text{ kJ}$ each) does this correspond to?

$$22 \text{ chocolate bars}$$

Solution

$$\begin{aligned} W &= 500 \text{ W} \cdot 24 \text{ h} = 12'000 \text{ Wh} = \\ &= 43'200'000 \text{ Ws} = 43'200 \text{ kWs} \quad \&= \quad 43'200 \text{ kJ} \quad \text{\text{Or: }} W \\ &= 0.5 \text{ kW} \cdot 24 \text{ h} = 12 \text{ kWh} = 43'200 \text{ kWs} \quad \&= \\ &= 43'200 \text{ kJ} \quad \text{\text{Or: }} n_{\text{bars}} = \frac{43'200 \text{ kJ}}{2'000 \text{ kJ}} = \\ &= 21.6 \text{ chocolate bars} \end{aligned}$$

Exercise E11 Conversions: Battery

2. How many minutes could a battery with 10 W be supplied by provided energy power for the calculated time?

Result

$$t = 200'000 \text{ min}$$

There are additional losses:

The battery W as a function of time t is $W = P \cdot t$. The power P is a function of the current I and the internal resistance r of the battery: $P = I^2 r$. The internal resistance r of the battery depends on the state of charge (SoC) of the battery.

- The wires also add additional losses to the system.

Exercise E12 Conversions: Speed, Energy, and Power

1. A vehicle speed of $80.00 \frac{\text{km}}{\text{h}}$ in $\frac{\text{m}}{\text{s}}$
 2. The energy of a 900 g battery is $1.6 \cdot 10^{-19} \text{ C}$
 3. The power of a 100 W light bulb is 100 W

Solution

Fast Solution:

```
\begin{align*} W &= 1.6 \cdot 10^{-19} \text{ C} \cdot 1.6 \cdot 10^{-19} \text{ V} = 2.56 \cdot 10^{-38} \text{ J} \\ \frac{1'000 \text{ m}}{3'600 \text{ s}} &= 80 \frac{\text{m}}{\text{s}} \quad \&= 22.22 \frac{\text{m}}{\text{s}} \\ P &= 100 \text{ W} = 100 \text{ J/s} = 100 \text{ W} \end{align*}
```

Exercise E13 Conversion: Vacuum Cleaner

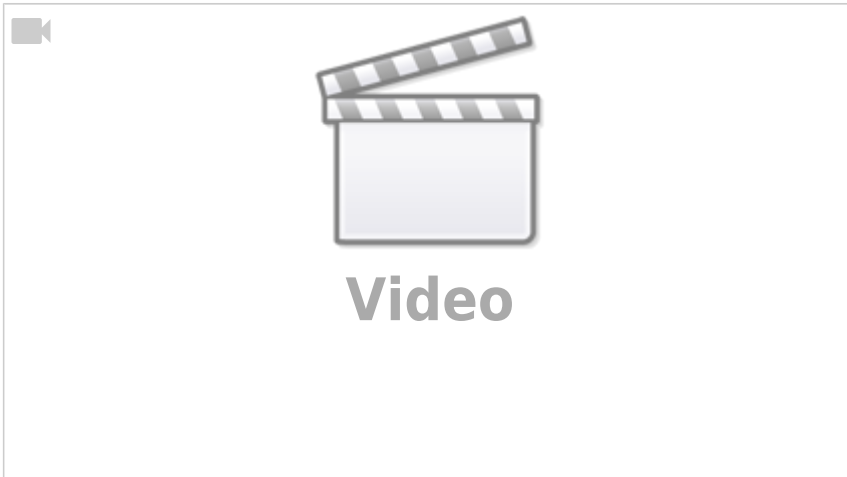
Your 18 V vacuum cleaner is equipped with a 4.0 Ah battery, it runs 15 min .

How much electrical power is consumed by the motor during this time on average?

Solution

```
\begin{align*} W &= 18 \text{ V} \cdot 4.0 \text{ Ah} = 72 \text{ Wh} \\ t &= 15 \text{ min} = 0.25 \text{ h} \\ P &= \frac{W}{t} = \frac{72 \text{ Wh}}{0.25 \text{ h}} = 288 \text{ W} \end{align*}
```

Exercise E14 Conversions: Video on Prefixes



Exercise E15 Conversion: Energy Consumption

Convert the following values step by step:

Result

How much energy does an average household consume per day when consuming an average power of \$ 500~{\rm W}\$ \$?

How many chocolate bars (\$2'000~{\rm kJ}\$ each) does this correspond to?

$$22~{\rm chocolate~bars}$$

Solution

$$\begin{aligned} W &= 500~{\rm W} \cdot 24~{\rm h} = 12000~{\rm Wh} = \\ 43'200'000~{\rm Ws} &= 43'200~{\rm kWs} \quad \&= 43'200~{\rm kJ} \quad \text{Or: } W \\ &= 0.5~{\rm kW} \cdot 24~{\rm h} = 12~{\rm kWh} = 43'200~{\rm kWs} \quad \&= \\ 43'200~{\rm kJ} \quad \&= \frac{43'200~{\rm kJ}}{2'000~{\rm kJ}} = \\ 21.6~{\rm chocolate~bars} \end{aligned}$$

Exercise E16 Conversion: Energy, Power and Area

2. The car battery is a lead-acid battery (12V) with a capacity of 60Ah (1080Wh). Average 100~{\rm m}

Result: ... and an usable battery capacity of \$60~{\rm kWh}\$\$. Solar panels produces per \$1~{\rm m}^2\$ in average in December \$0.2~{\rm kWh/m^2}\$\$. The car is driven \$50~{\rm km}\$ \$ per day. The size of a distinct solar module with \$460~{\rm W_p}\$ \$ (Watt peak) is \$1.9~{\rm m} \times 1.1~{\rm m}\$ \$.

$$A = 192.40~{\rm m^2} \quad \&= 22.96~{\rm m^2} \quad \&= 22.96~{\rm m^2}$$

.. What is the average power consumption of the car per day?

Solution

$$\begin{aligned} A &= \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2 \\ A &= \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2 \\ A &= \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2 \end{aligned}$$

Exercise E17 Conversion: Energy, Power and Area

1. What is the average power consumption of the car per day? The car has a battery capacity of 60 kWh. Solar panels produce per 1 m² in average in December 0.2 kWh. The car is driven 50 km per day. The size of a distinct solar module with 460 W_p (Watt peak) is 1.9 m (times 1.1 m).

$$A = \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2$$

2. What is the average power consumption of the car per day?

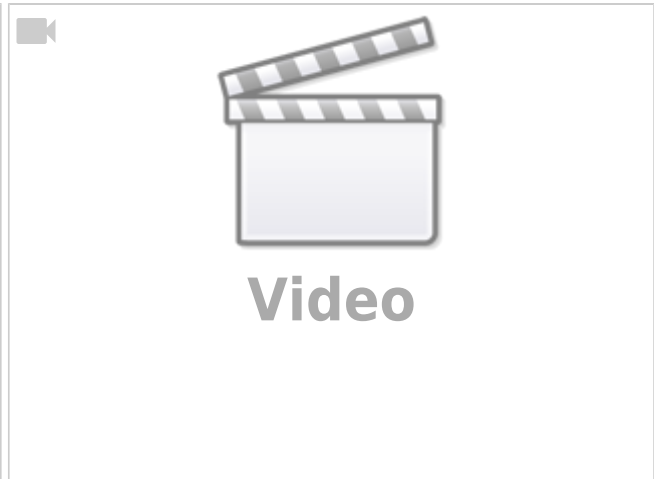
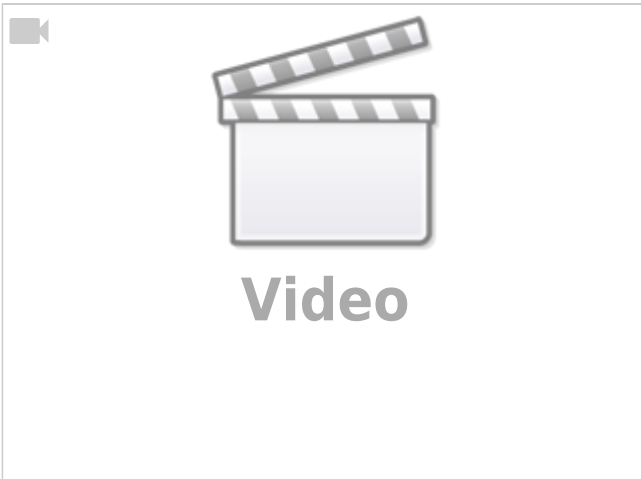
$$\begin{aligned} A &= \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2 \\ A &= \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2 \\ A &= \frac{100 \text{ panels} \cdot 1 \text{ kWh} \cdot 0.2 \text{ kWh/m}^2}{40 \text{ kWh/m}^2 \cdot 1 \text{ panel}} = 0.5 \text{ m}^2 \end{aligned}$$

$$\begin{aligned} \{W\} &= \frac{16 \text{ kWh}}{100 \text{ km}} = 0.16 \text{ kWh/km} \\ \{W\} &= \frac{16 \text{ kWh}}{100 \text{ km}} = 0.16 \text{ kWh/km} \\ \{W\} &= \frac{16 \text{ kWh}}{100 \text{ km}} = 0.16 \text{ kWh/km} \end{aligned}$$

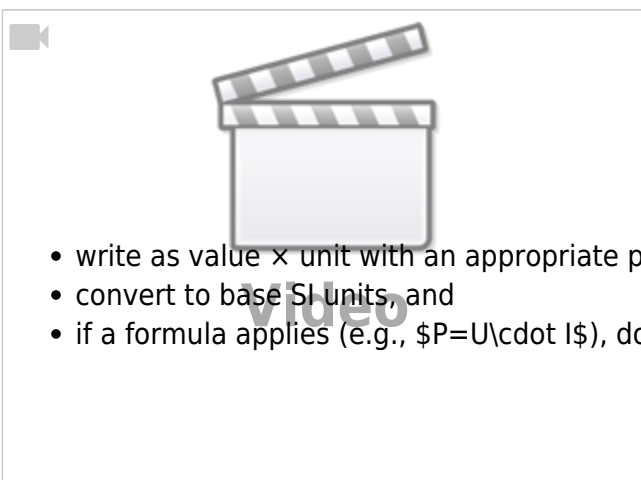
Embedded resources

A nice 10-minute intro into some of the main topics of this chapter

Short presentation of the SI units



Orders of magnitude and why prefixes matter.



Mini-assignment / homework (optional)

List 10 everyday EE-relevant quantities (e.g., USB current, phone battery energy, LED forward voltage). For each:

- write as value × unit with an appropriate prefix,
- convert to base SI units, and
- if a formula applies (e.g., $P=U \cdot I$), do a unit check.

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