

# Exam Summer Semester 2021

## Student Group

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# Exam Summer Semester 2021

## Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

## Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
  
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

## Tasks

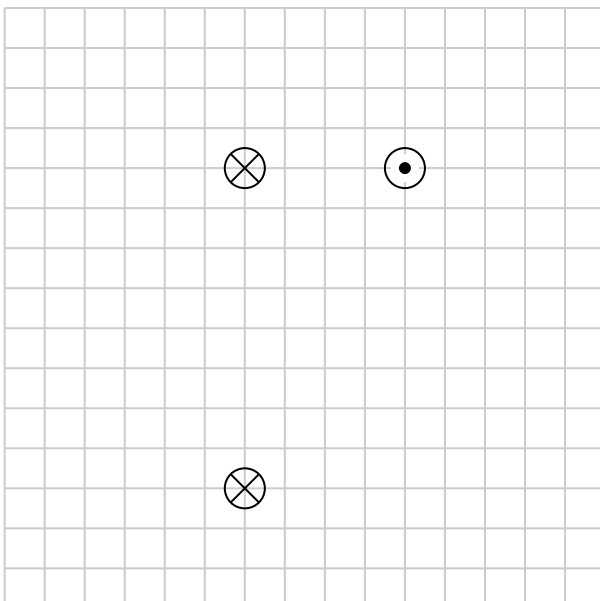
### Exercise E2 Magnetic Field Lines

(written test, approx. 4 % of a 120-minute written test, SS2021)

Several parallel conductors are projecting out of the plane.

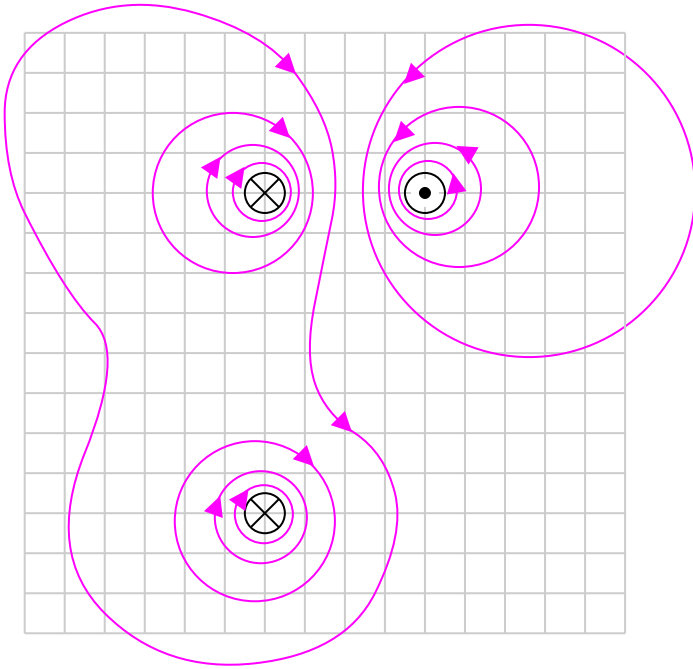
The same current  $I$  flows through all the conductors in different directions (see image below).

Sketch at least 10 field lines of the magnetic field strength  $\vec{H}$  in such a way that the different properties of the field lines (e.g. direction and density) can be seen.



Result

- high density of field lines near the conductors
- direction of the field lines given by the right-hand rule
- magnetic field has closed field lines
- resulting field given by superposition of field lines



**Exercise E4 Magnetic Flux Density**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

A) The electric motor is operated for an experiment in the laboratory. A rod is  $l = 100 \text{ cm}$  with a current of  $I = 100 \text{ A}$  is operated.

What is the distance to the rod and the current in the wire? (3 points, independent).  
 The figure below shows the top view of the laboratory with the supply line between A and B.

Path  $B = 0.12 \text{ m}$   
 $\mu_0 = 4\pi \cdot 10^{-7} \text{ Vs/Am}$ ,  $\mu_r = 1$

The formula for the magnetic field strength can be rearranged: 
$$H = \frac{I}{2\pi \cdot r} \quad || \quad r = \frac{I}{2\pi \cdot H}$$

Again, the magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$   
 Therefore: 
$$r = \frac{\mu_0 \mu_r I}{2\pi B} \quad || \quad = \frac{4\pi \cdot 10^{-7} \text{ Vs/Am} \cdot \{100 \text{ A}\}}{2\pi \cdot 100 \cdot 10^{-6}}$$

```
{~\rm T}}}} \\ \end{align*}
```

a) What is the highest magnetic flux density through the line in your body? (3 points)

Path

The magnetic field strength for a conducting wire is given as:

$$\begin{align*} H &= \frac{I}{2\pi \cdot r} \end{align*}$$

The magnetic flux density  $B$  is given as:  $B = \mu_0 \mu_r H$

Here, the maximum current is  $\hat{I} = 100 \text{ ~\rm A}$  and the distance to the cable is  $r = \sqrt{(0.1 \text{ ~\rm m})^2 + (0.4 \text{ ~\rm m})^2} = 0.412... \text{ ~\rm m}$ .

$$\begin{align*} B &= 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1 \\ &\cdot \frac{100 \text{ ~\rm A}}{2\pi \cdot 0.412... \text{ ~\rm m}} \end{align*}$$

**Exercise E5 Toroidal Coil**  
**(written test, approx. 5 % of a 120-minute written test, SS2021)**

A magnetic field with a flux density of at least  $50 \text{ mT}$  is to be achieved in a ring-shaped coil (toroidal coil).

The coil has 60 turns, wound around soft iron with  $\mu_r = 1200$ .

The average field line length in the coil should be  $l = 12 \text{ cm}$ .

$I_{\text{min}} = 4 \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}}$



What is the minimum current that must flow through a single winding?

Path

The magnetic field strength of a toroidal coil is given as:

$$H = \frac{N \cdot I}{l}$$

Based on the flux density the magnetic field strength can be derived by  $B = \mu_0 \mu_r \cdot H$ .

By this, the formula can be rearranged:

$$H = \frac{N \cdot I}{l} \iff \frac{B}{\mu_0 \mu_r} = \frac{N \cdot I}{l} \iff I = \frac{B \cdot l}{\mu_0 \mu_r \cdot N}$$

Putting in the numbers:

$$I = \frac{0.05 \text{ T} \cdot 0.12 \text{ m}}{4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 1'200 \cdot 60} = 0.6631... \frac{\text{T} \cdot \text{m}}{\frac{\text{Vs}}{\text{Am}}} = 0.6631... \frac{\text{Vs}}{\text{m}^2} \cdot \text{m} \cdot \frac{\text{Vs}}{\text{Am}} = 0.6631... \text{ A}$$

**Exercise E7 Cylindrical Coil**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

A) The magnetic flux (2 points) Information is given:

Result

- Length  $l = 30 \text{ cm}$ ,

Path • Winding diameter  $d = 390 \text{ mm}$ ,

- Number of windings  $N = 240$ ,
- Current in the conductor  $I = 500 \text{ mA}$ ,
- Material inside: Air

•  $\mu_0 = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}}$   
 The magnetic field strength is  $B = \mu_0 \mu_r \cdot H$ :

The proportion of the magnetic voltage outside the coil can be neglected. Determine the following for the inside of the coil:

$$\Phi = B \cdot A = \mu_0 \mu_r \cdot H \cdot A$$

a) Determine the magnetic field strength (2 points)  
 Putting in the numbers:  $B = 4\pi \cdot 10^{-7} \frac{\text{Vs}}{\text{Am}} \cdot 240 \cdot 0.5 \text{ A} = 0.0005026... \frac{\text{Vs}}{\text{m}^2}$

$$A = \pi r^2 = \pi \left( \frac{d}{2} \right)^2$$

Path

Therefore:  $\Phi = B \cdot \pi \left( \frac{d}{2} \right)^2$

Putting in the numbers:  $\Phi = 0.0005026... \frac{\text{Vs}}{\text{m}^2} \cdot \pi \left( \frac{0.39 \text{ m}}{2} \right)^2 = 0.00006004... \text{ Vs}$

Putting in the numbers:  $H = \frac{240 \cdot 0.5 \text{ A}}{0.3 \text{ m}}$

**Exercise E10 effect of induction**  
**(written test, approx. 5 % of a 120-minute written test, SS2021)**

A single conductor loop is penetrated by a changing magnetic flux.  
 The following figure shows the variation of the flux  $\Phi(t)$  over time.

Calculate the variation of the induced voltage  $u_{\text{ind}}(t)$  over time and draw it in a separate diagram.

ssu...inssL...

ss\..inss\...

**Path**

Based on Faraday's Law of Induction the induced voltage is given by: 
$$u_{\text{ind}} = - \frac{d}{dt} \Psi(t) = - \frac{d}{dt} \Phi(t)$$

For a linear function, the derivative can be substituted by Deltas ( $d \rightarrow \Delta$ ):  

$$u_{\text{ind}} = - \frac{\Delta \Phi(t)}{\Delta t} = - \frac{\Phi(t_{n+1}) - \Phi(t_n)}{t_{n+1} - t_n}$$

For a piece-wise linear function, the induced voltage can be calculated for each interval.  
 Here, there are 5 different intervals - in the following called  $I$  to  $V$  from

left to right:

$\dots$

- For the intervals  $I$ ,  $III$ , and  $V$ , the flux  $\Phi(t)$  is constant. Therefore,  $\Delta \Phi(t) = 0$  and  $u_{\text{ind}}(t) = 0$ .

- \$\$\dots\$\$...
- For the interval  $\Delta t$ :
    - The change in the flux is:  $\Delta \Phi(t) = 1.5 \cdot 10^{-4} \text{ Vs} - 4.5 \cdot 10^{-4} \text{ Vs} = -3.0 \cdot 10^{-4} \text{ Vs}$
    - The time span is:  $0.2 \text{ s}$
    - Conclusively, the induced voltage is:  $u_{\text{ind}}(t) = + \frac{3.0 \cdot 10^{-4} \text{ Vs}}{0.2 \text{ s}} = 1.5 \text{ mV}$

- For the interval  $\text{IV}$ :
  - The change in the flux is:  $\Delta \Phi(t) = 0 \cdot 10^{-4} \text{ Vs} - 1.5 \cdot 10^{-4} \text{ Vs} = -1.5 \cdot 10^{-4} \text{ Vs}$
  - The time span is:  $0.2 \text{ s}$
  - Conclusively, the induced voltage is:  $u_{\text{ind}}(t) = + \frac{1.5 \cdot 10^{-4} \text{ Vs}}{0.2 \text{ s}} = 0.75 \text{ mV}$

\$\$\dots\$\$

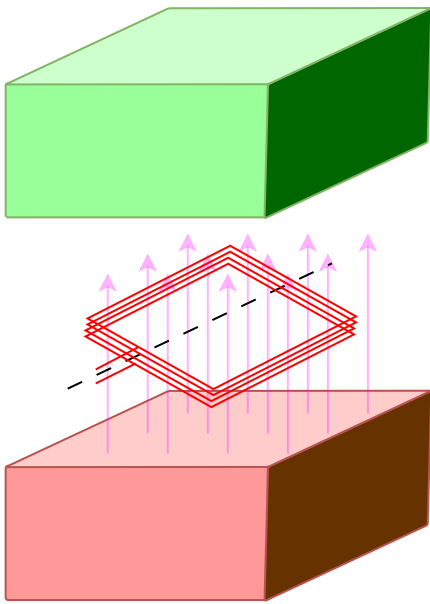
### Exercise E11 Coil in a magnetic Field (written test, approx. 4 % of a 120-minute written test, SS2021)

A coil with  $n = 300$  turns and a cross-sectional area  $A = 600 \text{ cm}^2$  is located in a homogeneous magnetic field.

The rotation of the coil causes a sinusoidal change in the magnetic field in the coil with the frequency  $f = 80 \text{ Hz}$ .

The maximum value of the magnetic flux density in the coil is  $\hat{B} = 2 \cdot 10^{-6} \text{ Vs/cm}^2$ .  

$$u_{\text{ind}} = -181 \text{ V} \cdot \cos(503 \text{ s}^{-1} \cdot t)$$



Derive the formula for the voltage induced in the coil and calculate the voltage amplitude.

Path

The induced voltage  $u_{\text{ind}}$  is given by:

$$u_{\text{ind}} = - \frac{d\Psi(t)}{dt} = - n \frac{d\Phi(t)}{dt}$$

With  $\Phi(t) = B(t) \cdot A$ , where  $A$  is the constant area of a single winding and  $B(t)$  is the changing field through this winding.

Due to the rotation, the field changes as:

$$B(t) = \hat{B} \cdot \sin(\omega t + \varphi) = \hat{B} \cdot \sin(2\pi f \cdot t + \varphi)$$

$$u_{\text{ind}} = - n \frac{d}{dt} (A \hat{B} \sin(2\pi f \cdot t + \varphi)) = - n \cdot A \hat{B} \cdot 2\pi f \cdot \cos(2\pi f \cdot t + \varphi)$$

The absolute value of the factor in front of the  $\cos$  is the maximum induced voltage  $\hat{U}_{\text{ind}}$ :

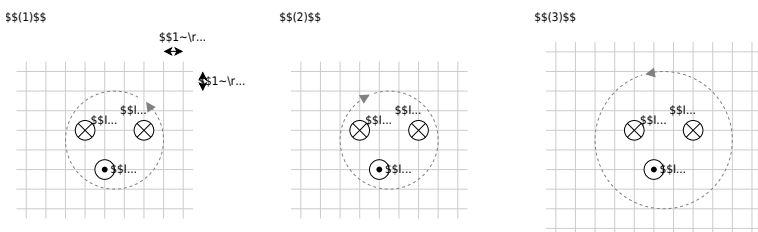
$$\hat{U}_{\text{ind}} = n \cdot A \cdot \hat{B} \cdot 2\pi f = 300 \cdot 0.06 \text{ m}^2 \cdot 2 \cdot 10^{-2} \text{ T} \cdot 2\pi \cdot 80 \text{ s}^{-1} = 180.95... \text{ V}$$

**Exercise E12 Magnetic Voltage**  
**(written test, approx. 6 % of a 120-minute written test, SS2021)**

The following images show cross-sections of electrical cables. Resulted path is shown as a dashed line. The magnetic voltage  $\theta$  on these paths shall be analyzed.

The following values are given for the currents:

- $I_1 = 5 \text{ A}$
- $I_2 = 2 \text{ A}$
- $I_3 = 1 \text{ A}$
- $I_4 = 4 \text{ A}$



Specify which magnetic voltages  $\theta_{(1)}$ ,  $\theta_{(2)}$ , and  $\theta_{(3)}$  result. Note the direction of the path in each case!

Path

For the resulting current the direction of the path has to be considered with the right-hand rule:

- $I_{(1)} = +I_2 - I_1 - I_3 \quad \rightarrow \quad \theta_{(1)} = 2 \text{ A} - 5 \text{ A} - 1 \text{ A}$
- $I_{(2)} = +I_3 + I_4 - I_1 \quad \rightarrow \quad \theta_{(2)} = 1 \text{ A} + 4 \text{ A} - 5 \text{ A}$
- $I_{(3)} = +I_3 - I_4 - I_2 \quad \rightarrow \quad \theta_{(3)} = 1 \text{ A} - 4 \text{ A} - 2 \text{ A}$

### Exercise E15 Lorentz Force (hard!) (written test, approx. 10 % of a 120-minute written test, SS2021)

A) ~~300 picture below shows straight high voltage line where the direction is shown as the result. A component of  $F = (1/20) \text{ N}$  of the resulting force is? (Independent)~~

A homogeneous geomagnetic field is assumed. The magnetic field strength has a vertical component of  $B_{\text{v}} = 40 \text{ } \mu\text{T}$  and a horizontal component of  $B_{\text{h}} = 20 \text{ } \mu\text{T}$ .

~~Only 10/100/7/9 is perpendicular to  $\vec{B}_{\text{v}}$  and to  $\vec{B}_{\text{h}}$  and points in the right direction by the right-hand rule.~~

The picture on the right shows the line (black), the field strength components, and the angle in front and top view for illustration purposes.

a) Calculate the force that results from the current flow on the entire conductor.  
 First, calculate the vertical and horizontal components and combine them accordingly.

Path  
 Top View

Path

The force on the transmission line can be calculated via the Lorentz force

$$\vec{F} = I \cdot (\vec{l} \times \vec{B})$$

- The horizontal component  $F_h$  of the force is based on the vertical component  $B_v$  of the magnetic field.
- The vertical component  $F_v$  of the force is based on the horizontal component  $B_h$  of the magnetic field.

Here, we have two components for the current and therefore for the force - to evaluate.

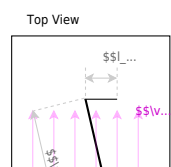
Considering the right-hand rule (and the cross product), the vertical field  $B_v$  generates a horizontal force  $F_h$  and vice versa.

The **horizontal component** is given by



$$\begin{align*}
 F_{\text{h}} &= l \cdot (l \cdot B_{\text{v}}) = 1'200 \text{ m} \cdot 300 \text{ m} \cdot 10^3 \text{ m} \cdot 40 \cdot 10^{-6} \frac{\text{Vs}}{\text{m}^2} = 14'400 \text{ N} \\
 F_{\text{As}} &= 14'400 \text{ N} \quad F_{\text{Ws}} = 14'400 \text{ N}
 \end{align*}$$

For the **vertical component** the angle  $\alpha$  has to be considered.  
 For the maximum  $F_{\text{v}}$  the angle  $\alpha$  has to be  $90^\circ$ , therefore the  $\sin$  has to be used.



$$F_{\text{v}} = l \cdot l \cdot B_{\text{h}} \cdot \sin \alpha = 1'200 \text{ m} \cdot 300 \text{ m} \cdot 10^3 \text{ m} \cdot 40 \cdot 10^{-6} \frac{\text{Vs}}{\text{m}^2} \cdot \sin 20^\circ = 2'462.545... \text{ N}$$

For the **overall force**  $F$  the Pythagorean theorem has to be used:

$$F = \sqrt{F_{\text{v}}^2 + F_{\text{h}}^2} = \sqrt{(14'400 \text{ N})^2 + (2'462.545... \text{ N})^2} = 14'609.04... \text{ N}$$

### Exercise E17 Impedance Characteristics

(written test, approx. 6 % of a 120-minute written test, SS2021)

A coil has an inductive reactance of  $X_0 = X(f_0) = 80 \text{ } \Omega$  at a frequency  $f_0 = 60 \text{ kHz}$ .

Calculate the frequencies  $f_1$ ,  $f_2$ ,  $f_3$  at which the following reactances are measured:

- $X_1 = 50 \text{ } \Omega$
- $f_1 = 37.5 \text{ kHz}$
- $X_2 = 121 \text{ } \Omega$
- $f_2 = 90.75 \text{ kHz}$
- $X_3 = 147 \text{ } \Omega$
- $f_3 = 110.25 \text{ kHz}$

Path

There are multiple ways to solve this question.

One way would be, to calculate the inductance  $L$  first by rearranging  $X(f) = 2\pi \cdot f \cdot L$ .

Another way uses ratios (or “rule of three”), since  $X(f) = f \cdot k$  with a constant  $k$ .

Therefore one can set up two formulas  $X_n = f_n \cdot k$ ,  $X_0 = f_0 \cdot k$ , and divide the formulae by each other.

This leads to: 
$$\begin{aligned} \frac{X_n}{X_0} &= \frac{f_n}{f_0} \quad \parallel \quad f_n = \frac{X_n}{X_0} \cdot f_0 \\ \frac{X_n}{X_0} \cdot f_0 &= \frac{f_0}{X_0} \cdot X_n \end{aligned}$$

Putting in the numbers: 
$$\begin{aligned} f_n &= \frac{60 \text{ kHz}}{80 \text{ } \Omega} \cdot X_n \\ &= 0.75 \frac{\text{ } \Omega}{\text{kHz}} \cdot X_n \end{aligned}$$

### Exercise E19 Complex series circuit

(written test, approx. 8 % of a 120-minute written test, SS2021)

A) Determine the absolute value of  $\underline{Z}_C$  if  $R = 200 \text{ } \Omega$  and  $\omega = 40 \text{ kHz}$  in the series circuit using a impedance vector diagram. Pay attention to the correct dimensioning.

a) Determine the complex impedance  $\underline{Z}_C$ .

Result

Path

$$\underline{Z}_C = -j \cdot 804 \, \Omega$$

The complex impedance  $\underline{Z}_C$  is given as

$$\underline{Z}_C = \frac{1}{j \cdot 2\pi \cdot f \cdot C} = \frac{-j}{2\pi \cdot 40 \cdot 10^3 \cdot 4.95 \cdot 10^{-9}} = -j \cdot 803.81 \dots \, \Omega$$

Based on the diagram:  $|\underline{Z}| = 828 \, \Omega$

**Exercise E21 Component Parameters**  
**(written test, approx. 10 % of a 120-minute written test, SS2021)**

Determine the component parameters  $R_M$  (motor resistance) and  $L_M$  (motor inductance) from the next exercises considering the following:  
 The values of the series resistance  $R_M$  and the inductance  $L_M$  are to be determined below. Both results in the impedance  $Z$  was applied.

This resulted in the recorded current of

a) Derive in general the equation for the absolute value of the impedance of the motor.

$$|\underline{Z}| = \sqrt{(2\pi \cdot f \cdot L_M)^2 + R_M^2}$$

Path

b) Determine the absolute values of the impedances from the specified RMS values at  $f_1$  and  $f_2$  (independent).  
 This has the advantage that  $R_M$  will cancel out:

$$Z_2^2 - Z_1^2 = (2\pi \cdot f_2 \cdot L_M)^2 + R_M^2 - \left( (2\pi \cdot f_1 \cdot L_M)^2 + R_M^2 \right)$$

The complex impedance  $\underline{Z}$  for a resistive inductive load is  $\underline{Z} = jX_L + R_M$   
 Path series circuit is given as

$$\underline{Z} = j \cdot 2\pi \cdot f \cdot L_M + R_M$$

Now we can rearrange to  $L_M^2$ :  
 The Pythagorean theorem can derive the absolute value:

$$L_M^2 = \frac{Z_2^2 - Z_1^2}{(2\pi \cdot f_2)^2 - (2\pi \cdot f_1)^2}$$

$$L_M = \frac{\sqrt{Z_2^2 - Z_1^2}}{2\pi \cdot \sqrt{f_2^2 - f_1^2}}$$

And then to  $L_M$ :

$$L_M = \frac{1}{2\pi} \sqrt{\frac{Z_2^2 - Z_1^2}{f_2^2 - f_1^2}}$$

With the values:

$$L_M = \frac{1}{2\pi} \sqrt{\frac{(10 \, \Omega)^2 - (6.25 \, \Omega)^2}{(100 \, \text{s}^{-1})^2 - (50 \, \text{s}^{-1})^2}} = 14.346 \dots \, \text{mH}$$

The resistance value  $R_M$  can be derived from  $Z^2 = (2\pi \cdot f_2 \cdot L_M)^2 + R_M^2 \implies R_M^2 = Z^2 - (2\pi \cdot f_2 \cdot L_M)^2 \implies R_M = \sqrt{Z^2 - (2\pi \cdot f_2 \cdot L_M)^2}$

The values have to be inserted also for  $R_M$ :  $R_M = \sqrt{(10 \cdot \Omega)^2 - (2\pi \cdot 100 \cdot 0.014346 \cdot \text{H})^2} = 4.3301 \cdot \Omega$

**Exercise E23 Signal Analysis**  
(written test, approx. 6 % of a 120-minute written test, SS2021)

**A) Determine the frequency, the amplitude values  $\hat{u}$ ,  $\hat{i}$  and the RMS values  $U$ ,  $I$  if the following signals are available in the consumer arrow system. (hard)**

- $u(t) = 50 \cdot \cos(6000 \cdot t + 4)$
- $i(t) = 30 \cdot \sin(6000 \cdot t + 5)$

**Result**

a) Determine the angular frequency  $\omega$  and the RMS values  $U$ ,  $I$

- $f = 955 \text{ Hz}$

The frequency can be derived by the term in the sine function:  $\omega = 6000 \text{ s}^{-1}$   
 The amplitude values  $\hat{u} = 50 \text{ V}$ ,  $\hat{i} = 30 \text{ A}$  are given directly by the coefficient of the sine and cosine functions.  
 The RMS values:  $U = \frac{\hat{u}}{\sqrt{2}} = 35.4 \text{ V}$ ,  $I = \frac{\hat{i}}{\sqrt{2}} = 21.4 \text{ A}$

For the phase  $\varphi$ , we have to subtract  $\varphi_i$  from  $\varphi_u$ .  
 But to get these values, both the  $u(t)$  and  $i(t)$  need to have the same sinusoidal function! Therefore:  
 •  $\varphi_u = 4$   
 •  $\varphi_i = 5$   
 For the RMS values of sinusoidal functions the amplitudes have to be multiplied with  $\frac{1}{\sqrt{2}}$

By this we get for  $\varphi$ :  $\varphi = \varphi_u - \varphi_i = 4 - 5 = -1 \text{ rad} = -57.3^\circ$

Converted in degree:  $\varphi = -1 \cdot \frac{360^\circ}{2\pi} = -57.3^\circ$

**Exercise E25 Resonant Circuit**  
(written test, approx. 4 % of a 120-minute written test, SS2021)

**C) In a resonant circuit, the inductance  $L$  and the capacitance  $C$  are fixed. The resistance  $R$  can be varied.**

Path  $U_{\text{rms}} = 12 \sqrt{2} \sin(2\pi f_0 t)$   
 $R = 200 \Omega$   
 •  $L = 20 \text{ mH}$   
 •  $C = 30 \mu\text{F}$   
 For the following calculation, the internal resistance  $R_i$  and the resistance  $R$  have to be combined:  $R_{\Sigma} = R_i + R$

Here, either one knows that the gain factor  $Q$  stands for  $Q = \frac{U_C}{U_{\text{rms}}}$  and therefore can directly use the following formula:  $Q = \frac{U_C}{U_{\text{rms}}} = \frac{1}{R_{\Sigma}} \sqrt{\frac{L}{C}}$   
 $R_{\Sigma} = \frac{U_{\text{rms}}}{U_C} \sqrt{\frac{L}{C}}$

When the gain factor is not known, one has to derive it:  
 The voltage  $U_C$  at resonance is only given by the total ohmic resistance  $R_{\Sigma}$  and the source voltage  $U_{\text{rms}}$ :  $I = \frac{U_{\text{rms}}}{R_{\Sigma}}$

This current flow also through the impedance of the capacitor  $U_C = Z_C \cdot I = \frac{1}{\omega C} \cdot I = \frac{U_{\text{rms}}}{\omega C R_{\Sigma}}$

At resonance, the angular frequency  $\omega$  is given by  $\omega = \frac{1}{\sqrt{LC}}$   
 $U_C = \frac{U_{\text{rms}}}{\frac{1}{\sqrt{LC}} C R_{\Sigma}} = \frac{U_{\text{rms}} \sqrt{LC}}{R_{\Sigma}}$   
 $R_{\Sigma} = \frac{U_{\text{rms}} \sqrt{LC}}{U_C}$

a) What is the resonance frequency  $f_0$ ?

In both cases, we end up with the same formula, where we have to insert the physical values:  $R_{\Sigma} = \frac{U_{\text{rms}}}{U_C} \sqrt{\frac{L}{C}} = \frac{1}{4} \sqrt{\frac{20 \cdot 10^{-3}}{30 \cdot 10^{-6}}} = 6.4549 \dots \Omega$   
 The resonant frequency  $f_0$  is given as  $f_0 = \frac{1}{2\pi \sqrt{LC}} = \frac{1}{2\pi \sqrt{20 \cdot 10^{-3} \cdot 30 \cdot 10^{-6}}} = 205.4681 \dots \text{ Hz}$

**Exercise E27 Multiphase systems (written test, approx. 4 % of a 120-minute written test, SS2021)**

1) Specify the RMS value of the phase voltage  $U_{\text{rms}}$  and the line voltage  $U_{\text{line}}$ .  
 Result:

A voltage with the RMS value  $U_{\text{rms}} = 110 \text{ V}$  is applied between the terminals

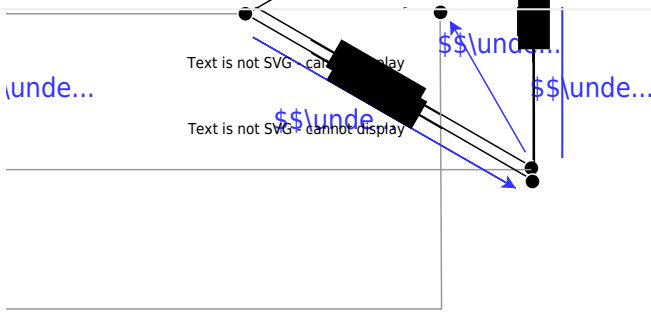
On each winding.

Through each of the windings, there is a current with an RMS value  $I_{\text{RMS}} = 5 \text{ A}$  and a phase shift of  $\varphi = +25^\circ$  compared to the voltage.

- $U_{\text{RMS}} = 5110 \text{ V}$
- $U_{\text{L}} = 8160 \text{ V}$

a) Draw the circuit diagram of  $U_{\text{RMS}} = 5110 \text{ V}$  as applied between the terminals of the winding, by raising the winding voltage  $u(t)$  to the value  $U_{\text{RMS}} \cdot \sqrt{2} \cdot \sin(\omega t)$ . For the calculation,  $P_{\text{Set}} = 3 \text{ A} \cdot \sqrt{2} \cdot 110 \text{ V} \cdot \cos(25^\circ) = 210 \text{ W}$  and  $U_{\text{L}} = \sqrt{3} \cdot U_{\text{RMS}} = 8160 \text{ V}$ . The result must be zero:  $\sum_{i=1}^3 P_i = 0$ .

By this (and showing in the example in the image below), One can see, that  $I_{\text{L}} = \sqrt{3} \cdot I_{\text{RMS}} = \sqrt{3} \cdot 5 \text{ A}$



one single phase as an example



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Last update: **2026/01/12 00:06**

