

Exam Winter Semester 2022

Student Group

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Exam Winter Semester 2022

Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

Tasks

Exercise E2 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

A heating element made of nichrome wire with a temperature coefficient of $1.80 \cdot 10^{-3} \text{ K}^{-1}$ is electric

Result power dissipation (= heat flow) of $P = 40 \text{ W}$ is necessary.

Determine the current I needed for operation.

The Nichrome wire has a resistivity of $1.10 \cdot 10^{-6} \Omega \text{ m}$.

The heating element is 3 m long and has a diameter of 3.57 mm .

Calculate the resistance R of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad | \quad \text{with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \& \quad | \quad R = 1.10 \cdot 10^{-6} \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

[resistivity](#), [power](#), [exam ee1 ws2022](#)

Exercise E4 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. The grid below explains how the effect of a tax sensitive company's earnings on its share value has a Resulted in a \$10 million increase in the price of its shares at \$25 a share. Give an answer.

Its temperature coefficients are: $\alpha = 0.01 \sim \{1\} \over \{\rm K\}}$ and $\beta = 71 \cdot 10^{-6} \sim \{1\} \over \{\rm K^2\}$

Result The temperature inside the refrigeration system can reach down to $-40\text{ }^{\circ}\text{C}$.

$$R_s = 65 \text{ } \Omega$$

The power transfer is electric $P_{\text{end}} = \dot{Q}_{\text{cool}} \left(1 + \frac{1}{\text{COP}} \right)$ and the cooling heat $\dot{Q}_{\text{cool}}$. Therefore, a solution is to use a heat float up the refrigeration system.

Therefore, with constant ΔU and increasing R the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad \& | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} \quad \& | \\ R &= 10 \sim \text{m}\{\text{k}\} \cdot \Omega \cdot \left((1 + 0.01 \sim \frac{1}{\text{m}\{\text{K}\}}) \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\}) + 71 \cdot 10^{-6} \sim \frac{1}{\text{m}\{\text{K}\}^2} \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\})^2 \right) \end{aligned}$$

temperature dependent resistance, power, heat, exam ee1 ws2022

Exercise E6 Pure Resistor Network Simplification

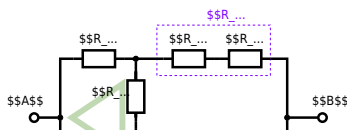
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall in with \$ close 200 at 0 late the \$ 2 a R = 1 5 0 t a n O e s a m d n s b e t w e n
Result Assigned. \$ \rm B\$.

Solution

$$R \approx 132.8 \sim \Omega$$

Now a wye-delta transformation is necessary.



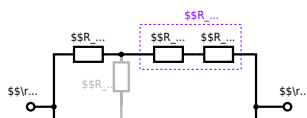
Since $R_2 = R_3$ and based on the equations for the transformation, the transformed R_Y is given as:
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega) \parallel$$

1. The switch shall now be open. Calculate the equivalent resistance R_{eq} between A and B .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega)$$

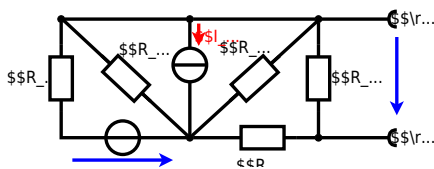
$$R_{eq} = \frac{(500 \, \Omega \cdot 200 \, \Omega)}{500 \, \Omega + 200 \, \Omega}$$

network simplification, exam ee1 ws2022

Exercise E8 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.
Result

$$U_s = U_{AB} = 4.5 \, \text{V} \quad R_i = R_{AB} = 6 \, \Omega$$

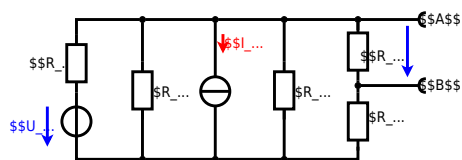


Calculate the internal resistance R_i and the source voltage U_s of an equivalent linear voltage source on the connectors A and B.

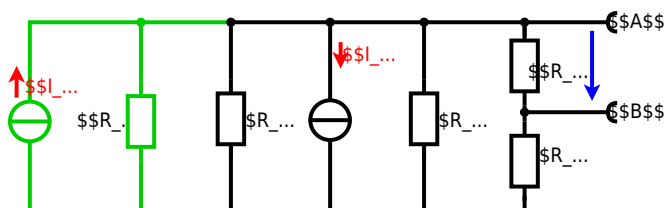
$R_1 = 5.0 \, \Omega$, $U_2 = 6.0 \, \text{V}$, $R_3 = 10 \, \Omega$, $I_4 = 4.2 \, \text{A}$, $R_5 = 10 \, \Omega$, $R_6 = 7.5 \, \Omega$, $R_7 = 15 \, \Omega$ Use equivalent sources in order to simplify the circuit!

Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of U_2 and R_1 can be transformed into a current source $I_2 = \frac{U_2}{R_1}$ and R_1 :



Now a lot of them can be combined. The resistors R_1 , R_3 , R_5 are in parallel, like also I_2 and I_4 :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_{24}}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the U_{24} is calculated by I_{24} as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$I_{24} = \frac{U_{24}}{R_6 + R_1 \parallel R_3 \parallel R_5} = \frac{(U_1 - I_4) \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by R_{135} , R_6 , and R_7 .

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = (U_1 - I_4) \cdot \frac{R_7 \cdot R_1 \parallel R_3 \parallel R_5}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance R_i the ideal voltage source is substituted by its resistance (0Ω , so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with $R_1 \parallel R_3 \parallel R_5 = 5 \Omega \parallel 10 \Omega \parallel 10 \Omega = 5 \Omega \parallel 5 \Omega = 2.5 \Omega$:

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \quad R_{AB} = 15 \Omega \parallel (7.5 \Omega + 2.5 \Omega)$$

dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E10 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (shown in the figure) consists of a DC voltage source $U = 12 \text{ V}$, a resistor $R_1 = 2 \text{ M}\Omega$, a capacitor $C = 10 \text{ nF}$, and a resistor $R_2 = 1 \text{ M}\Omega$. The switch S_1 is initially open. The voltage across the capacitor is again 0 V at the moment $t_0 = 0 \text{ s}$ when the switch S_1 is closed. Calculate the voltage $u_C(t_2)$ across the capacitor at $t_2 = 1 \text{ ms}$ after closing the switch.

Solution: To solve this, first create an equivalent linear voltage source from U , R_1 , and R_2 .

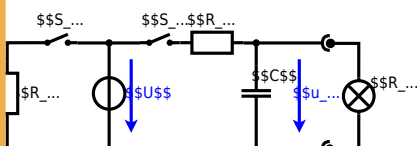
$$U_{eq} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12 \text{ V} \cdot 1 \text{ M}\Omega}{2 \text{ M}\Omega + 1 \text{ M}\Omega} = 4 \text{ V}$$

$$R_{eq} = R_1 \parallel R_2 = \frac{2 \text{ M}\Omega \cdot 1 \text{ M}\Omega}{2 \text{ M}\Omega + 1 \text{ M}\Omega} = \frac{2}{3} \text{ M}\Omega$$

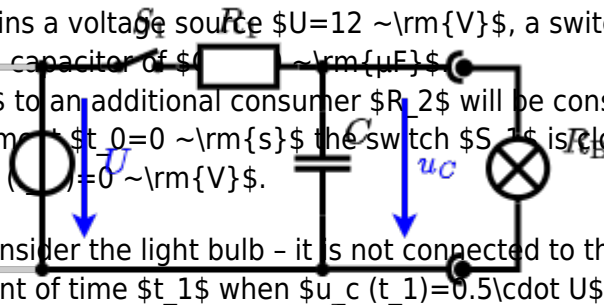
Solution: The voltage across the capacitor is given by $u_C(t) = U_{eq} \cdot (1 - e^{-t/\tau})$ with $\tau = R_{eq} \cdot C$.

$$u_C(t_2) = 4 \text{ V} \cdot (1 - e^{-t_2/\tau}) = 4 \text{ V} \cdot (1 - e^{-1 \text{ ms} / (\frac{2}{3} \text{ M}\Omega \cdot 10 \text{ nF})})$$

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting R_2 .

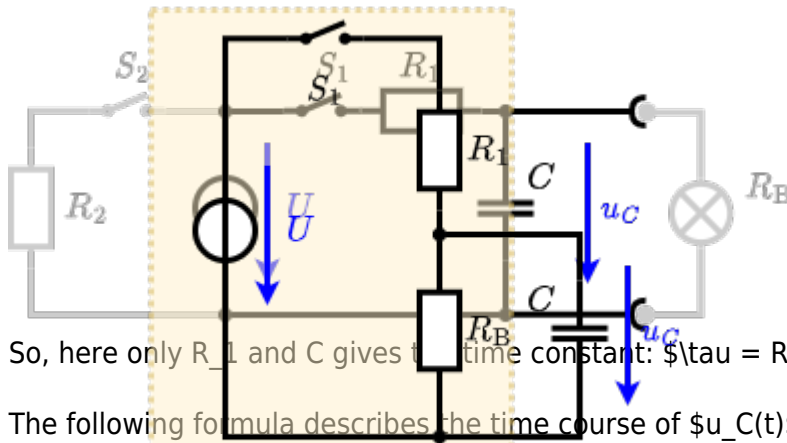


The circuit contains a voltage source $U=12\text{ V}$, a switch S_1 , a resistor of $R_1=20\text{ }\Omega$ and a capacitor of $C=100\text{ }\mu\text{F}$. The switch S_2 to an additional consumer R_2 will be considered to be open for the first task. At the moment $t_0=0\text{ s}$ the switch S_1 is closed, the voltage across the capacitor is $u_C(t_0)=0\text{ V}$.



First do not consider the light bulb - it is not connected to the RC circuit. Calculate the point of time t_1 when $u_C(t_1)=0.5 \cdot U$.

Solution



So, here only R_1 and C gives the time constant: $\tau = R_1 \cdot C$

The following formula describes the time course of $u_C(t)$ which has to be $u_C(t_1)=0.5 \cdot U$:
$$u_C(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to $(1 - e^{-t/\tau}) = 0.5$. An equivalent linear voltage source can be given with $U_s = U \cdot \frac{R_B}{R_1 + R_B}$ and $R_i = R_1 \parallel R_B$ as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: $U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$. The internal resistance is given by substituting the ideal voltage source with its resistance ($=0\text{ }\Omega$, short-circuit).
$$R_i = R_1 \parallel R_B = 10\text{ }\Omega$$

$$u_C(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1\text{ ms}/(10\text{ }\Omega \cdot 100\text{ }\mu\text{F})})$$

charging capacitors, dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

Exercise E12 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)

2. Calculate the phasor impedance $\underline{Z}$ of the circuit shown in the figure. The result $\underline{Z}$ shall be given.

After analysis, the full expression for the impedance $\underline{Z}$ shall be extracted and written in the form $\underline{Z} = \frac{1}{2} + j\frac{1}{2} + 5j\text{ }\Omega$.

Solution Calculate the physical values of the two components.

$$C = 103 \sim \mu\text{F}$$

$$R = 0.12 \sim \Omega$$

Solution

The current and voltage are in phase once there is only a pure ohmic (= pure real)

$$\underline{I} = \frac{\underline{U}}{\underline{Z}}$$

Therefore, over complex impedance a capacitor with the same absolute value of

$$\underline{Z} = j\omega L = -j\omega C$$

$$\omega L = \omega C$$

$$\omega = 2\pi \cdot f = 2\pi \cdot 4.68 \sim \text{MHz} = 29.96 \sim 10^7 \text{ s}^{-1}$$

$$L = \frac{1}{\omega C} = \frac{1}{29.96 \sim 10^7 \text{ s}^{-1} \cdot 103 \sim 10^{-6} \text{ F}} = 3.34 \sim 10^{-13} \text{ H} = 3.34 \sim 10^{-13} \text{ H}$$

The absolute value of the impedance can be calculated as:

$$|\underline{Z}| = \sqrt{R^2 + (\omega L)^2}$$

$$|\underline{Z}| = \sqrt{0.12^2 + (3.34 \sim 10^{-13} \text{ H} \cdot 29.96 \sim 10^7 \text{ s}^{-1})^2} = 3.34 \sim 10^{-13} \text{ H}$$

$$C = \frac{1}{\omega L} = \frac{1}{29.96 \sim 10^7 \text{ s}^{-1} \cdot 3.34 \sim 10^{-13} \text{ H}} = 1.03 \sim 10^{-6} \text{ F} = 1.03 \sim \mu\text{F}$$

The phase φ_i can be calculated as:

$$\varphi_i = \arctan\left(\frac{\omega L}{R}\right) = \arctan\left(\frac{3.34 \sim 10^{-13} \text{ H} \cdot 29.96 \sim 10^7 \text{ s}^{-1}}{0.12 \sim \Omega}\right) = 0.24 \sim \text{rad}$$

complex impedance, exam ee1 ws2022

Exercise E14 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

Exercise E14 The resistor values $R_1 = 1.00 \sim \Omega$, $R_2 = 10.0 \sim \Omega$ and $R_3 = 1.00 \sim \Omega$ are connected in a series circuit.

Result: With $f = 4.70 \sim \text{MHz}$, the high-pass characteristic of the circuit is such that the voltage across the resistor R_1 shall have the same absolute value of the impedance as a capacitor $C_1 = 40 \sim \text{nF}$ at $f_1 = 4 \sim \text{MHz}$.

Solution

$$R_1 = 1.00 \sim \Omega$$

$$R_2 = 10.0 \sim \Omega$$

A series circuit means that the current is constant on every component.

The equivalent impedance for R and L combined is given by:

$$\underline{Z} = R + j\omega L$$

$$|\underline{Z}| = \sqrt{R^2 + (\omega L)^2}$$

$$|\underline{Z}| = \sqrt{R^2 + (\omega L)^2}$$

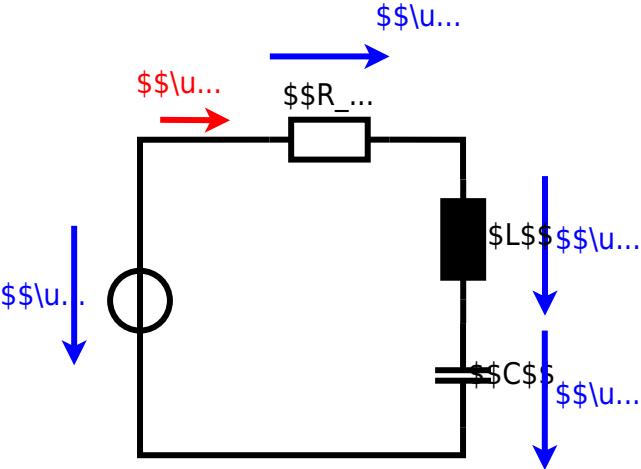
Therefore, the resulting current of the parallel circuit is given as:

$$|\underline{I}| = \frac{|\underline{U}|}{|\underline{Z}|}$$

$$|\underline{I}| = \frac{|\underline{U}|}{\sqrt{R^2 + (\omega L)^2}}$$

$$|\underline{I}| = \frac{|\underline{U}|}{\sqrt{R^2 + (\omega L)^2}}$$

$$|\underline{I}| = \frac{|\underline{U}|}{\sqrt{R^2 + (\omega L)^2}}$$



complex impedance, exam ee1 ws2022

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