

# Exam Winter Semester 2022

## Student Group

| First Name | Surname | Matrikel Nr. |
|------------|---------|--------------|
|            |         |              |
|            |         |              |
|            |         |              |

## Table of Contents

|                                                                                                                   |    |
|-------------------------------------------------------------------------------------------------------------------|----|
| <b>Exam Winter Semester 2022</b>                                                                                  | 2  |
| Additional permitted Aids                                                                                         | 2  |
| Hits                                                                                                              | 2  |
| Tasks                                                                                                             | 2  |
| Exercise E2 Resistance of a Wire by Resistivity (written test, approx. 6 % of a 60-minute written test, WS2022)   | 2  |
| Exercise E4 Temperature-dependent Resistance (written test, approx. 6 % of a 60-minute written test, WS2022)      | 2  |
| Exercise E6 Pure Resistor Network Simplification (written test, approx. 13 % of a 60-minute written test, WS2022) | 3  |
| Exercise E8 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)             | 5  |
| Exercise E10 Charging Capacitors (written test, approx. 16 % of a 60-minute written test, WS2022)                 | 9  |
| Exercise E12 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)        | 10 |
| Exercise E14 Impedances at different Frequencies (written test, approx. 18 % of a 60-minute written test, WS2022) | 11 |
| Exercise E16 Complex Impedance Circuit (written test, approx. 15 % of a 60-minute written test, WS2022)           | 12 |

# Exam Winter Semester 2022

## Additional permitted Aids

- non-programmable calculator,
- formulary (2 DIN A4 pages)

## Hits

- The duration of the exam is 60 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.

## Tasks

### Exercise E2 Resistance of a Wire by Resistivity

(written test, approx. 6 % of a 60-minute written test, WS2022)

A heating element made of nichrome wire with a temperature coefficient of  $1.80 \cdot 10^{-3} \text{ K}^{-1}$  and an electric power dissipation (= heat flow) of  $P = 40 \text{ W}$  is necessary.

Calculate the current  $I$  needed for operation.

The Nichrome wire has a resistivity of  $1.10 \cdot 10^{-6} \text{ } \Omega \text{ m}$ .

The heating element is  $3 \text{ m}$  long and has a diameter of  $3.57 \text{ mm}$ .

Calculate the resistance  $R$  of the heating element.

Solution

$$\begin{aligned} P &= U \cdot I = R \cdot I^2 \quad \rightarrow \quad I = \sqrt{\frac{P}{R}} \\ \sqrt{\frac{P}{R}} &= \sqrt{\frac{40 \text{ W}}{0.33 \text{ } \Omega}} \end{aligned}$$

$$\begin{aligned} R &= \rho \cdot \frac{l}{A} \quad \& \quad | \text{ with } A = r^2 \cdot \pi = \frac{1}{4} d^2 \cdot \pi \\ R &= \rho \cdot \frac{l}{\frac{1}{4} d^2 \cdot \pi} \quad \& \quad R = 1.10 \cdot 10^{-6} \text{ } \Omega \text{ m} \cdot \frac{4 \cdot 3 \text{ m}}{(3.57 \cdot 10^{-3} \text{ m})^2 \cdot \pi} \end{aligned}$$

[resistivity](#), [power](#), [exam ee1 ws2022](#)

### Exercise E4 Temperature-dependent Resistance

(written test, approx. 6 % of a 60-minute written test, WS2022)

2. The grid below explains 2.6. Give a factor that is sensitive to the magnitude of  $\alpha$  and is not sensitive to the magnitude of  $\beta$ . Result:  $\alpha$  is the effect of  $\alpha$  on  $\beta$ . Give an answer for  $\alpha$  and  $\beta$  at  $\alpha = 25$  and  $\beta = 10$ .

Its temperature coefficients are:  $\alpha = 0.01 \sim \{1\} \over \{\rm K\}}$  and  $\beta = 71 \cdot 10^{-6} \sim \{1\} \over \{\rm K^2\}$

**Result** The temperature inside the refrigeration system can reach down to  $-40\text{ }^{\circ}\text{C}$ .

$R_s = 6.5 \times 10^{-4} \Omega$

The power transfer is electric  $P_{\text{end}} = \dot{Q}_{\text{cool}} \left( 1 + \frac{1}{\text{COP}} \right)$  and the condenser heat  $\dot{Q}_{\text{cond}}$  is therefore, a solution is to use a thermoelectric heat pump to heat up the refrigeration system.

Therefore, with constant  $\Delta U$  and increasing  $R$  the power decreases. Ten times more resistance decreases the heat flow to one-tenth.

$$\begin{aligned} R &= R_0 \cdot (1 + \alpha \cdot \Delta T + \beta \cdot \Delta T^2) \quad \& | \\ \text{with } \Delta T &= T_{\text{end}} - T_{\text{start}} \quad \& | \\ R &= 10 \sim \text{m}\{\text{k}\} \cdot \Omega \cdot \left( (1 + 0.01 \sim \frac{1}{\text{m}\{\text{K}\}}) \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\}) + 71 \cdot 10^{-6} \sim \frac{1}{\text{m}\{\text{K}\}^2} \cdot (-40 \sim ^\circ \text{m}\{\text{C}\} - 25 \sim ^\circ \text{m}\{\text{C}\})^2 \right) \end{aligned}$$

temperature dependent resistance, power, heat, exam ee1 ws2022

## Exercise E6 Pure Resistor Network Simplification

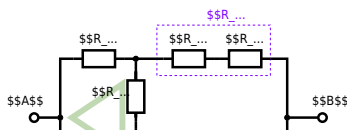
(written test, approx. 13 % of a 60-minute written test, WS2022)

The following shall in with \$ close 200 at 0 late the \$ 2 a R = 1 6 1 0 a n o n s g a n d o s b e t w e n  
Result Assigned. \$ \rm B\$.

### Solution

$$R \approx 132.8 \sim \Omega$$

Now a wye-delta transformation is necessary.



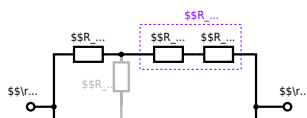
Since  $R_2 = R_3$  and based on the equations for the transformation, the transformed  $R_Y$  is given as: 
$$R_Y = \frac{R_2 \cdot R_2}{R_2 + R_2 + R_2} = \frac{(100 \, \Omega)^2}{3 \cdot 100 \, \Omega} = \frac{1}{3} \cdot 100 \, \Omega = 33.33 \, \Omega$$

The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{\text{eq}} = R_Y + (R_Y + R_1 + R_1) \parallel (R_Y + R_2) \parallel R_{\text{eq}} = 33.33 \, \Omega + (33.33 \, \Omega + 400 \, \Omega) \parallel (33.33 \, \Omega + 100 \, \Omega)$$

1. The switch shall now be open. Calculate the equivalent resistance  $R_{\text{eq}}$  between  $A$  and  $B$ .

Solution



The equivalent resistor is given by a parallel configuration of resistors in series:

$$R_{eq} = (R_2 + R_1 + R_1) \parallel (R_2 + R_2) \parallel (100 \, \Omega + 200 \, \Omega + 200 \, \Omega) \parallel (100 \, \Omega + 100 \, \Omega) \parallel (500 \, \Omega) \parallel (200 \, \Omega)$$

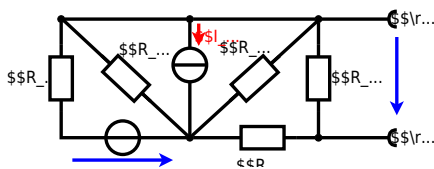
$$R_{eq} = \frac{(500 \, \Omega \cdot 200 \, \Omega)}{500 \, \Omega + 200 \, \Omega}$$

network simplification, exam ee1 ws2022

### Exercise E8 Equivalent linear Source (written test, approx. 14 % of a 60-minute written test, WS2022)

The circuit in the following has to be simplified.  
Result

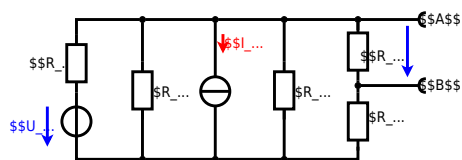
$$U_s = U_{AB} = 4.5 \, \text{V} \quad R_i = R_{AB} = 6 \, \Omega$$



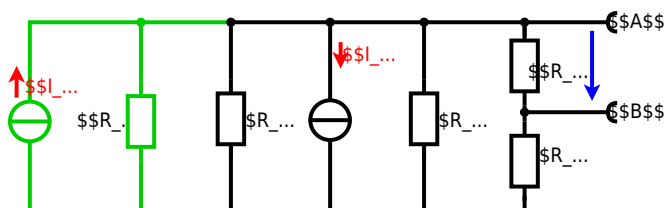
Calculate the internal resistance  $R_{\text{int}}$  and the source voltage  $U_{\text{S}}$  of an equivalent linear voltage source on the connectors  $\text{A}$  and  $\text{B}$ .  
 $R_1 = 5.0 \, \Omega$ ,  $U_2 = 6.0 \, \text{V}$ ,  $R_3 = 10 \, \Omega$ ,  $I_4 = 4.2 \, \text{A}$ ,  
 $R_5 = 10 \, \Omega$ ,  $R_6 = 7.5 \, \Omega$ ,  $R_7 = 15 \, \Omega$  Use equivalent sources in order to simplify the circuit!

### Solution

The best thing is to re-think the wiring like rubber bands and adjust them:



The linear voltage source of  $U_2$  and  $R_1$  can be transformed into a current source  $I_2 = \frac{U_2}{R_1}$  and  $R_1$ :



Now a lot of them can be combined. The resistors  $R_1$ ,  $R_3$ ,  $R_5$  are in parallel, like also  $I_2$  and  $I_4$ :

$$R_{135} = R_1 || R_3 || R_5$$

$$I_{24} = I_2 - I_4 = \frac{U_2}{R_1} - I_4$$

The resulting circuit can again be transformed:



Here, the  $U_{24}$  is calculated by  $I_{24}$  as the following:

$$U_{24} = I_{24} \cdot R_{135}$$

$$I_{24} = \frac{U_{24}}{R_6 + R_1 \parallel R_3 \parallel R_5}$$

On the right side of the last circuit, there is a voltage divider given by  $R_{135}$ ,  $R_6$ , and  $R_7$ .

$$U_{AB} = U_{24} \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5} = \left( \frac{U_{24}}{R_1} - I_{44} \right) \cdot \frac{R_7}{R_6 + R_7 + R_1 \parallel R_3 \parallel R_5}$$

For the internal resistance  $R_i$  the ideal voltage source is substituted by its resistance ( $0 \Omega$ , so a short-circuit):

$$R_{AB} = R_7 \parallel (R_6 + R_1 \parallel R_3 \parallel R_5)$$

with  $R_1 \parallel R_3 \parallel R_5 = 5 \Omega \parallel 10 \Omega \parallel 10 \Omega = 5 \Omega \parallel 5 \Omega = 2.5 \Omega$ :

$$U_{AB} = \frac{6.0 \text{ V}}{5.0 \Omega} - 4.2 \Omega \cdot \frac{15 \Omega \cdot 2.5 \Omega}{7.5 \Omega + 15 \Omega + 2.5 \Omega} \quad R_{AB} = 15 \Omega \parallel (7.5 \Omega + 2.5 \Omega)$$

dc network analysis, pure resistor network simplification, delta wye transformation, exam ee1 ws2022

### Exercise E10 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

The circuit (shown in the figure) consists of a DC voltage source  $U$ , a switch  $S_1$ , a capacitor  $C$ , and a resistor  $R_1$ . The voltage across the capacitor is again  $0 \text{ V}$  at the moment  $t_0 = 0 \text{ s}$  when the switch  $S_1$  is closed. Calculate the voltage  $u_C(t_2)$  across the capacitor at  $t_2 = 1 \text{ ms}$  after closing the switch.

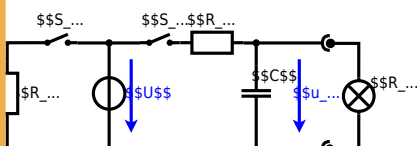
**Solution:** To solve this, first create an equivalent linear voltage source from  $U$ ,  $R_1$ , and  $R_2$ .

$$U_{eq} = \frac{U \cdot R_2}{R_1 + R_2} = \frac{12 \text{ V} \cdot 2 \text{ k}\Omega}{1 \text{ k}\Omega + 2 \text{ k}\Omega} = 8 \text{ V}$$

$$R_{eq} = R_1 \parallel R_2 = \frac{1 \text{ k}\Omega \cdot 2 \text{ k}\Omega}{1 \text{ k}\Omega + 2 \text{ k}\Omega} = \frac{2}{3} \text{ k}\Omega$$

**Solution:** The voltage across the capacitor is given by  $u_C(t) = U_{eq} \left( 1 - e^{-\frac{t}{R_{eq}C}} \right)$ .

On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting  $R_2$ .





**Solution** Calculate the physical values of the two components.

$$C = 103 \sim \mu\text{F}$$

$$R = 0.12 \sim \Omega$$

**Solution**

The current and voltage are in phase once there is only a pure ohmic (= pure real)

$$\underline{I} = \frac{\underline{U}}{\underline{Z}}$$

Therefore, over complex impedance a capacitor with the same absolute value of

$$\underline{Z} = j\omega L = -j\omega C$$

$$\omega L = \omega C \Rightarrow L = C \Rightarrow L = 103 \sim \mu\text{H}$$

The absolute value of the impedance can be calculated as:

$$|\underline{Z}| = \sqrt{R^2 + (\omega L)^2} = \sqrt{0.12^2 + (2\pi \cdot 4.7 \cdot 10^6 \cdot 103 \cdot 10^{-6})^2} \approx 287.96 \sim \Omega$$

$$\varphi_i = \arctan\left(\frac{\omega L}{R}\right) = \arctan\left(\frac{287.96}{0.12}\right) \approx 89.77^\circ$$

complex impedance, exam ee1 ws2022

## Exercise E14 Impedances at different Frequencies

(written test, approx. 18 % of a 60-minute written test, WS2022)

**Exercise E14** The resistor values  $R_1 = 1.00 \sim \Omega$  and  $R_2 = 10.0 \sim \Omega$  are in a series circuit.

Result:  $R_1$  and  $R_2$  shall have the same absolute value of the impedance as a capacitor  $C_1 = 40 \sim \text{nF}$  at  $f_1 = 4 \sim \text{MHz}$ .

**Solution**

$$R_1 = 1.00 \sim \Omega$$

$$R_2 = 10.0 \sim \Omega$$

A series circuit means that the current is constant on every component.

The equivalent impedance for  $R$  and  $L$  combined is given by:

$$\underline{Z} = R + j\omega L$$

$$|\underline{Z}| = \sqrt{R^2 + (\omega L)^2}$$

Therefore, the resulting current of the parallel circuit is given as:

$$\underline{I} = \frac{\underline{U}}{\underline{Z}}$$

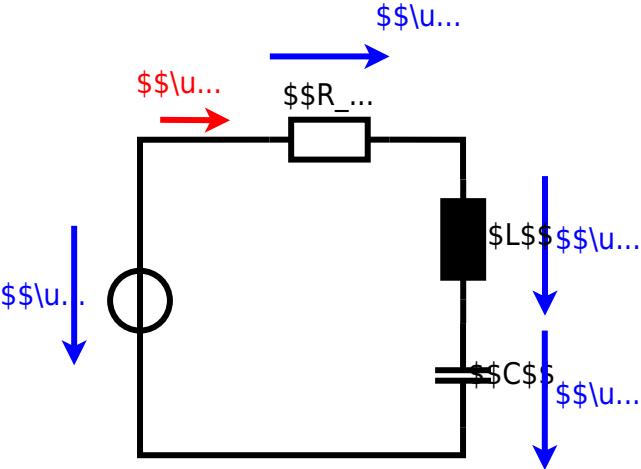
$$|\underline{I}| = \frac{|\underline{U}|}{|\underline{Z}|} = \frac{10 \sim \text{V}}{\sqrt{R^2 + (\omega L)^2}}$$

$$|\underline{I}|^2 = \frac{100}{R^2 + (\omega L)^2}$$

$$R^2 + (\omega L)^2 = \frac{100}{|\underline{I}|^2}$$







complex impedance, exam ee1 ws2022

From:

<https://first.mexle.te.hs-heilbronn.de/> - **MEXLE Wiki**

Permanent link:

[https://first.mexle.te.hs-heilbronn.de/electrical\\_engineering\\_and\\_electronics\\_1/ws2022\\_exam?rev=1768172558](https://first.mexle.te.hs-heilbronn.de/electrical_engineering_and_electronics_1/ws2022_exam?rev=1768172558)

Last update: **2026/01/12 00:02**

