

# Exam Winter Semester 2022

## Student Group

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# Exam Winter Semester 2022

## Additional permitted Aids

- non-programmable calculator,
- formulary (4 one-sided DIN A4 pages)

## Hits

- The duration of the exam is 120 min.
- Attempts to cheat will lead to exclusion and failure of the exam.
- Withdrawal is no longer possible after these exam has been handed out.
- Please write down intermediate calculations and results on the assignment sheet. (when more space is needed also on the reverse side. In this case: Mark it clearly).
- Always use units in the calculation.
- Use a document-proof, non-red pen.
- Sub-tasks, which are independently solvable are marked with: (independent)
- Sub-tasks, which are hard are marked with: (hard)

## Tasks

### Exercise E8 Charging Capacitors

(written test, approx. 16 % of a 60-minute written test, WS2022)

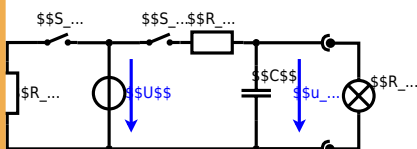
The circuit (with the realisation) is in the picture. For  $t < 0$  the switch  $S_1$  is open and the voltage across the capacitor is again  $0 \text{ V}$  at the moment  $t_0 = 0 \text{ s}$  when the switch  $S_1$  is closed. Calculate the voltage  $u_c(t_2)$  across the capacitor at  $t_2 = 1 \text{ ms}$  after closing the switch.

#### Resolution

Hint: To solve this, first create an equivalent linear voltage source from  $U$ ,  $R_1$ , and  $R_2$ .

Solution: The internal resistance is given by  $R_{int} = R_1 \parallel R_2 = \frac{R_1 R_2}{R_1 + R_2} = \frac{10 \cdot 20}{10 + 20} = \frac{200}{30} = \frac{20}{3} \Omega$ .

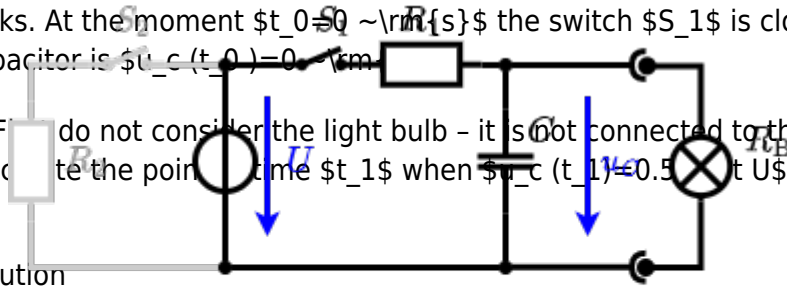
On an alternative view, one can try to create an equivalent linear voltage source again. Then, the internal resistance is given by substituting the ideal voltage source is again short-circuiting  $R_2$ .



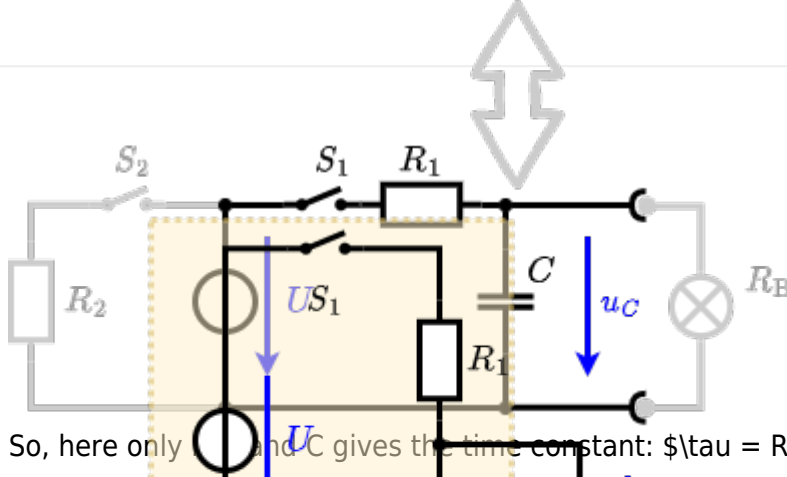
The circuit contains a voltage source  $U = 12 \text{ V}$ , a switch  $S_1$ , a resistor of  $R_1 = 20 \Omega$  and a capacitor of  $C = 100 \mu\text{F}$ . The switch  $S_2$  to an additional consumer  $R_2$  will be considered to be open for the first

asks. At the moment  $t_0 = 0 \text{ s}$  the switch  $S_1$  is closed, the voltage across the capacitor is  $u_c(t_0) = 0 \text{ V}$ .

1. Do not consider the light bulb - it is not connected to the RC circuit. Calculate the point in time  $t_1$  when  $u_c(t_1) = 0.5 \cdot U$ .



Solution



So, here only  $U$  and  $C$  gives the time constant:  $\tau = R_1 \cdot C$

The following formula describes the time course of  $u_C(t)$  which has to be  $u_c(t_1) = 0.5 \cdot U$ : 
$$u_c(t) = U \cdot (1 - e^{-t/\tau}) = 0.5 \cdot U$$
 It has to be rearranged to 
$$(1 - e^{-t/\tau}) = 0.5 \implies e^{-t/\tau} = 0.5 \implies -t/\tau = \ln(0.5) \implies t = \tau \cdot \ln(0.5)$$

An equivalent linear voltage source can be given with  $U$ ,  $R_1$ , and  $R_B$  as seen in yellow.

Therefore, the voltage of the equivalent linear voltage source is: 
$$U_s = U \cdot \frac{R_B}{R_1 + R_B} = \frac{1}{2} \cdot U$$
 The internal resistance is given by substituting the ideal voltage source with its resistance ( $R_i = 0 \Omega$ , short-circuit). 
$$R_i = R_1 \parallel R_B = 10 \Omega$$

$$u_c(t_2) = U_s \cdot (1 - e^{-t_2/(R_i \cdot C)}) = \frac{1}{2} \cdot U \cdot (1 - e^{-1 \text{ ms} / (10 \Omega \cdot 100 \mu\text{F})})$$

**Exercise E12 Impedances at different Frequencies**  
**(written test, approx. 18 % of a 60-minute written test, WS2022)**

2. A RC circuit with resistor values  $R_1 = 1 \text{ k}\Omega$  and  $R_2 = 10 \text{ k}\Omega$  is shown in the following circuit (of 3S)  $U = 10 \text{ V}$ .  
 Result:  $f = 200 \text{ kHz}$  has higher reactance than  $f = 50 \text{ kHz}$  through  $R_1$ .  
 A resistor  $R_1$  shall have the same absolute value of the impedance as a capacitor  $C = 40 \text{ nF}$  at  $f = 4 \text{ MHz}$ .

Solution

$$R_1 = 1.00 \Omega$$

**Solution**

A series circuit means that the current is constant on every component. Parallel circuit means that the voltage is the same on every component.

Equivalent impedance for the parallel combination of  $R_3$  and  $X_{L3}$  is:

$$\frac{1}{Z_{eq}} = \frac{1}{R_3} + \frac{1}{X_{L3}} = \frac{1}{R_3} + \frac{1}{j\omega L_3}$$

So it gets messy, that's perpendicular impedances can be simplified for  $X_{L3} = j\omega L_3 = j2\pi \cdot 60 \cdot 0.01 = j3.77 \Omega$  and  $R_3 = 4 \Omega$ . Therefore the resulting current of the parallel circuit is given as:

$$I_{3R} = \frac{U}{Z_{eq}} = \frac{U}{\sqrt{R_3^2 + X_{L3}^2}}$$

This can be rearranged to get  $R_3 = \sqrt{Z_{eq}^2 - X_{L3}^2}$

Back to the first formula:  $X_{L3} = j\omega L_3 = j2\pi \cdot 60 \cdot 0.01 = j3.77 \Omega$

$$I_{3R} = \frac{U}{\sqrt{R_3^2 + X_{L3}^2}} \Rightarrow R_3 = \sqrt{\left(\frac{U}{I_{3R}}\right)^2 - X_{L3}^2}$$

**Exercise E10 Analyzing complex Impedances (written test, approx. 14 % of a 60-minute written test, WS2022)**

2. Calculate the phase angle and the effective value of the current  $I$  in the circuit. The components ( $R$  and  $X_L$ ) shall be given.

After analysis, the full bridge circuit can be simplified to a single branch circuit in phase.  $Z_{total} = R + jX_L = 10 + j16 \Omega$

**Solution**

1. Calculation of the effective values of the components.

**Solution**  $I_{eff} = \frac{U_{eff}}{\sqrt{R^2 + X_L^2}} = \frac{50}{\sqrt{10^2 + 16^2}} = 2.6 \text{ A}$

**Solution**

The current  $I$  is a phasor. The voltage  $U$  is a phasor. The resulting current  $I$  is a phasor.

The phase angle  $\varphi$  is calculated as:

$$\varphi = \arctan\left(\frac{X_L}{R}\right) = \arctan\left(\frac{16}{10}\right) = 58^\circ$$

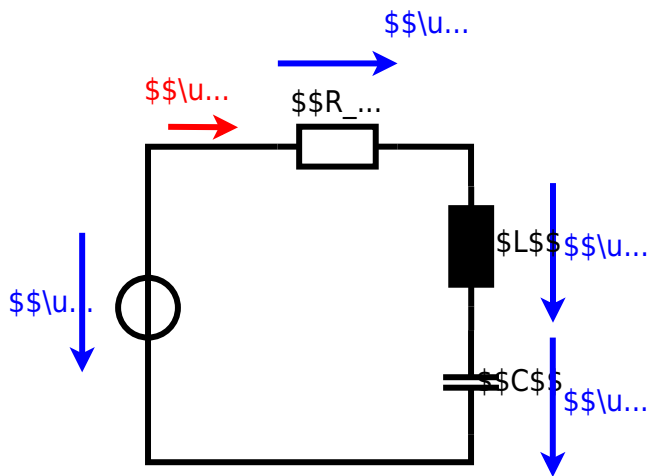
With the complex part comes the complex value  $Z = R + jX_L = 10 + j16 \Omega$

The phase angle  $\varphi$  can be calculated as:

$$\varphi = \arctan\left(\frac{\text{Im}(Z)}{\text{Re}(Z)}\right) = \arctan\left(\frac{16}{10}\right) = 58^\circ$$







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